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Eye-Blink Detection Using Facial Landmarks

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Eye-Blink Detection Using Facial Landmarks

Tereza Soukupová

May 26, 2016

DIPLOMA THESIS ASSIGNMENT

Student: Bc. Tereza Soukupová

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Title of Diploma Thesis: Eye-Blink Detection Using Facial Landmarks

Guidelines:

1. Propose an eye-blink detection algorithm that uses facial landmarks as an input.
2. Evaluate the proposed detector quantitatively based on the ground-truth dataset. Study the detector sensitivity on the image/video quality (especially on face resolution, video frame rate, head pose, or partial occlusions).
3. Prepare a demonstration of the proposed eye-blink detector and consider an application in the context of e.g., Human-Computer Interface, attention monitoring, drowsiness detection, etc.

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Author statement for undergraduate thesis

I declare that the presented work was developed independently and that I have listed all sources of information used within it in accordance with the methodical instructions for observing the ethical principles in the preparation of university theses.

Prague, 27 May 2016

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Abstract

A real-time algorithm to detect eye blinks in a video sequence from a standard camera is proposed. Recent landmark detectors, trained on in-the-wild datasets exhibit excellent robustness against face resolution, varying illumination and facial expressions. We show that the landmarks are detected precisely enough to reliably estimate the level of the eye openness. The proposed algorithm therefore estimates the facial landmark positions, extracts a single scalar quantity – eye aspect ratio (EAR) – characterizing the eye openness in each frame. Finally, blinks are detected either by an SVM classifier detecting eye blinks as a pattern of EAR values in a short temporal window or by hidden Markov model that estimates the eye states followed by a simple state machine recognizing the blinks according to the eye closure lengths. The proposed algorithm has comparable results with the state-of-the-art methods on three standard datasets.

Keywords

Eyes, eye blink, eye blink detector, face, landmarks, eye aspect ratio, EAR, SVM, HMM.

Abstrakt

Práce se zabývá detekcí mrkání očí ve videozáznamu pořízeném standardní webkamerou. V nedávné době byly představeny obličejové detektory na detekci a sledování významných bodů v obličeji. Tyto detektory dosahují výborných výsledků a jsou velmi robustní vůči různorodému osvětlení, rozlišení obličeje v obraze a výrazu v tváři. Ukážeme, že s pomocí těchto obličejových detektorů umíme spolehlivě odhadnout míru otevřenosti oka. Algoritmus tedy nejdříve odhadne významné body v obličeji, potom z těchto bodů vypočítá skalární hodnotu jako poměr výšky a šířky oka (eye aspect ratio EAR), která charakterizuje míru otevřenosti oka v každém snímku videosekvence. Mrknutí jsou pak detekována buď SVM klasifikátorem, který se naučí charakteristický vzor mrknutí z EAR hodnot v krátkém časovém úseku a nebo jsou mrknutí detekována skrytým Markovovým modelem, který v každém snímku určí, zda je oko zavřené nebo otevřené, a na základě délky mrknutí pak stavový automat rozpozná která zavření očí znamenala mrknutí. Navrhované metody pracují v reálném čase a dosahují srovnatelných výsledků se state-of-the-art.

Klíčová slova

Oči, mrkání, detektor mrkání, obličej, významné body v obličeji, EAR, SVM, HMM.

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1 Introduction

Detecting eye blinks is important for instance in systems that monitor a human operator vigilance, e.g. driver drowsiness [1], in systems that warn a computer user staring at the screen without blinking for a long time to prevent the dry eye and the computer vision syndromes [2, 3], in human computer interfaces that ease communication for disabled people [4], or for anti-spoofing protection in face recognition systems [5].

Many methods have been proposed to automatically detect eye blinks in a video sequence. The methods are more detailed in Sec. 3.1. Their major drawback is that they usually implicitly impose too strong requirements on the setup, in the sense of a relative face-camera pose (head orientation), image resolution, illumination, motion dynamics, etc. Especially the heuristic methods that use raw image intensity are likely to be very sensitive despite their real-time performance.

However nowadays, robust real-time facial landmark detectors [6, 7, 8] that capture most of the characteristic points on a human face image, including eye corners and eyelids, are available. Most of the state-of-the-art landmark detectors formulate a regression problem, where a mapping from an image into landmark positions or into other landmark parametrization is learned. These modern landmark detectors are trained on in-the-wild datasets and they are thus robust to varying illumination, various facial expressions, and moderate non-frontal head rotations. An average error of the landmark localization of a state-of-the-art detector is usually below five percent of the inter-ocular distance.

Therefore, we propose a simple but efficient algorithm to detect eye blinks by using a recent facial landmark detector. A single scalar quantity that reflects a level of the eye openness is derived from the landmarks. Finally, having a per-frame sequence of the eye openness estimates, the eye blinks are detected by two proposed methods. The first one finds blinks by an SVM classifier that is trained on examples of blinking and non-blinking patterns. The second method is unsupervised. It learns a Hidden Markov Model to estimate eye states. Eye blinks are then detected via simple state machine according to the blink duration. The blink detectors are evaluated on three standard blink datasets with ground-truth annotations.

A small study to measure blink properties such as frequency over time and duration is carried out. These characteristics are important to determine a degree of drowsiness. We define a *drowsiness index* as a function of blink frequency and blink duration. Finally the blink detection is applied and an experiment measuring a subject drowsiness during a day while working on a laptop is presented.

A structure of the work is following. You can read about eye blinking from physiological point of view in Chapter 2. Chapter 3 presents related work. Chapter 4 describes the proposed methods for blink detection. Experiments and testing of the proposed algorithms are described in Chapter 5. You can find our blink application determining drowsiness while using laptop in Chapter 6. There are implementation details in Chapter 7. Chapter 8 concludes the work.

2 Eye Blinks

2.1 What is eye blinking?

Eye blinking is partly subconscious fast closing and reopening of the eyelid. There are multiple muscles involved in eye blinking. Two main muscles are *orbicularis oculi* and *levator palpebrae superioris* that control the eye closing and opening.

The main purpose of eye blinking is to moisten an eye cornea. It also cleans the eye cornea when eyelashes do not capture all the dust and a dirt gets into the eye.

There are two types of unconscious blinking. The *spontaneous* blinking is done without any obvious external stimulus. It happens while breathing or digesting. The second type of involuntary blinking is called the *reflex* blinking. It is caused by contact with the cornea, fast visual change of light in front of the eye, sudden presence of near object or by a loud noise. Another type of blinking is the *voluntary* blinking which is invoked consciously under the control of the individual.

2.1.1 Parameters of blinks

There are two main parameters of blinking: frequency and duration. Average frequency of blinking of an adult is 15-20 blinks/min but there are only 2-4 blinks/min physiologically needed. Children have lower blink rate. Newborns even blink only 2× per minute. Interestingly, women using oral contraceptives blink 32% more often than other women [9]. The rate of spontaneous blinking can be increased by a strong wind, dry air conditions or by emotional situations. On the other hand, when the eyes are focused on an object for longer time (e.g. reading), the blink rate decreases to about 3-4 blinks/min.

Work [10] publishes a hypothesis that the blink frequency is increased by negative mood, stress, nervousness, fatigue, negative emotions, pain, boredom. On the other hand the frequency is decreased in positive states while relaxing, having pleasant feeling, after successful problem solving and also while reading and having greater attention.

The duration of blinking depends on an individual, usually it is about 100-400 ms. The *reflex* blinking is faster than the *spontaneous*. Blink frequency and duration can be affected by relative humidity, temperature, brightness or by fatigue, disease or physical activity.

3 Related work

3.1 State-of-the-art of blink detectors

Many of different methods have been developed for blink detection. We can divide them into several categories according to requirements on a setup and their performance. The output can be either open/closed eye recognition or a blink detection. The methods are divided as intrusive and non-intrusive. The intrusive methods require a special hardware on setup such as electrodes placed along the scalp to measure EOG [11], Doppler sensor [12, 13] or glasses with a special close-up cameras observing the eyes [14]. The non-intrusive optical methods can also use a special hardware such as illuminators or infrared cameras [15, 16, 17], but many modern approaches aim to have non-intrusive systems relying on a standard remote camera only.

The second group consists of non-intrusive vision-based techniques using only an RGB camera. They use either single image characteristics or they use several subsequent frames from a video sequence to detect a motion. They usually have three stages: a face detection, an eye region detection and a blink detection. Viola-Jones algorithm is mostly used for face detection.

The *single image* processing approaches are based e.g. on skin color segmentation [18], edge detection, a parametric model fitting to find the eyelids [19], or active shape models [20]. In [21] vertical intensity projections are used. The intensities are summed in a row and while supposing that eyebrow and the iris area are darker than skin. So, there are two projections minima and one maximum between them, see Fig. 3.1. A change of the projection curve during blinking is investigated. A method [22] is similar in spirit of using pixel intensities but histograms instead of projections are used. Another method [1] assumes that an open eye is horizontally symmetric, whereas a closed eye is not. The eye region is horizontally divided into upper and lower halves. On the basis of the cumulative sum of the intensities open and closed eye patterns are compared. There is a combination of two methods in [23]. An eye region to binary image is converted and morphological closure is done, see Fig. 3.2. Two features are computed: a cumulative difference of black pixels in successive images and a ratio of height to width of eye. An SVM on the basis of the two features mentioned previously is used to recognize if an eye is open or closed. Most of these methods are sensitive to illumination.

Another method for blink detection is based on template matching [24, 25, 26, 27]. The templates with open and/or closed eyes are learned and normalized cross correlation

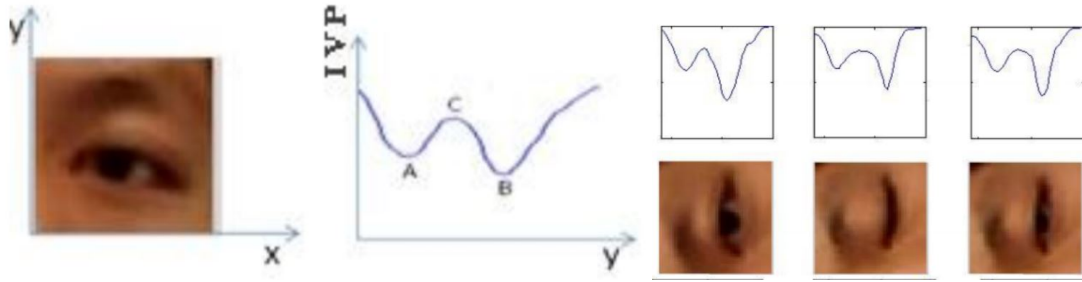


Figure 3.1 An example of intensity vertical projections from a method described in [21].



Figure 3.2 An example of binarized eye regions described in method [23].

coefficient R is computed for an eye region of each image:

$$R(x, y) = \frac{\sum_{x', y'} (T(x', y') - I(x + x', y + y'))^2}{\sqrt{\sum_{x', y'} T(x', y')^2 \sum_{x', y'} I(x + x', y + y')^2}}, \quad (3.1)$$

where I is original image, T is template image and x and y are pixel coordinates. The correlation score is then compared for open and closed eye template. In [25], a correlation only with open eye template is computed and a change of R in time is analyzed. A blink starts if two consecutive frames have R value lower then predefined threshold TL and ends if two consecutive frames have correlation coefficient greater than threshold TH . The goal is to detect voluntary blinks which are defined as blinks longer than 250 ms and shorter than 2 s. They do not have offline preprocessed template in [26] but the template is learned online at the beginning of a sequence. The examples of open eye templates can be seen in Fig. 3.3.



Figure 3.3 Open eye templates. Image taken from [26].

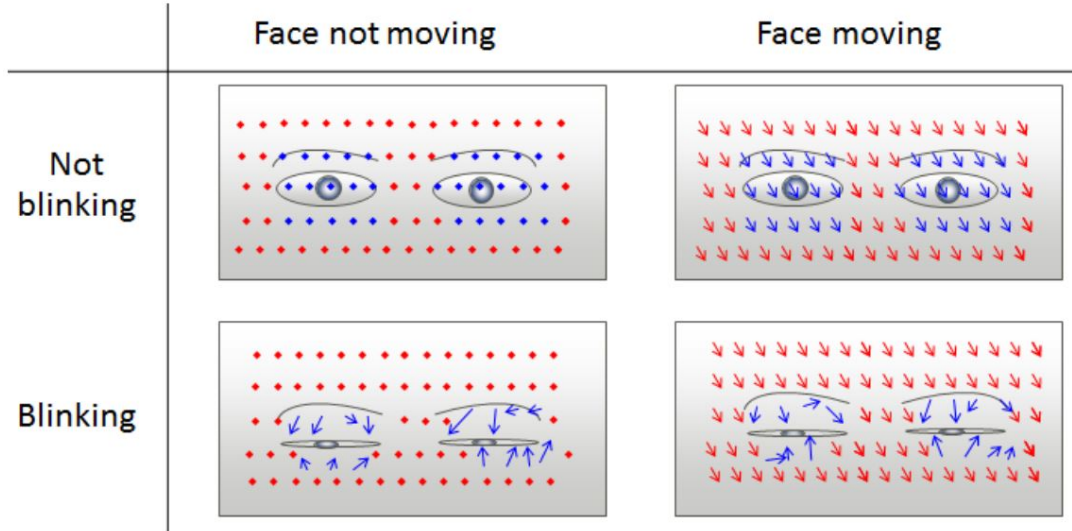


Figure 3.4 An example of facial and eyelids motion more described in [32].

There are many *motion based* methods which need two or more consecutive frames for frame differencing [28, 29]. A difference of two consecutive frames and application of morphological operations is done in paper [30]. A motion of eyelids is detected if a sum of intensities of the subtraction is greater than a given threshold. However, it is not known if an eye is open or closed after the motion. Thus, the frames differencing with analysis of the vertical and horizontal projections in binary image are combined. The methods using optical flow [31, 2] usually tend to estimate dominant movement direction and magnitude. A methods using similar motion analysis is described in [32]. A movement of a whole face must be distinguished and subtracted to capture the residual movement of the eyelids, see Fig. 3.4. Another method using motion analysis can be found in [33]. A histogram of oriented gradients is used for blink detection. A paper [34] combines a spatial and temporal derivatives which represent motion between frames. Only motion vectors in vertical direction are analyzed. Another motion approach is described in work [3]. There are about 255 KLT trackers in an eye region divided into 3×3 cells. A local average motion is computed from KLT trackers belonging to each cell. The eye blink is detected by a state machine if a downward movement occurs and the upward movement is present no later than 150 ms. A workflow of the proposed eye blink detector is shown in Fig. 3.5. In [35] a similar approach is used. It is supposed, that all the motion vectors for each pixel are similar to each other in magnitude and orientation during head movement in contrast with the eye blink movement where motion vectors differ. So a state machine is set up and a blink is detected based on mean values and standard deviations of vertical components of vector motions. The state machine also takes a time spent in a closed state into account.

There are two similar methods to ours using facial landmarks. A paper [20] presents a method where Active Shape Model is used to obtain 98 facial landmarks, 8 of them

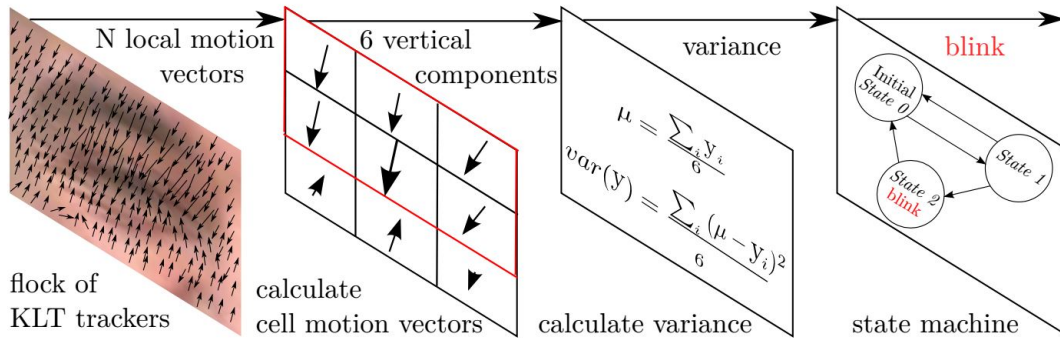


Figure 3.5 An example of motion based method described in work [3].

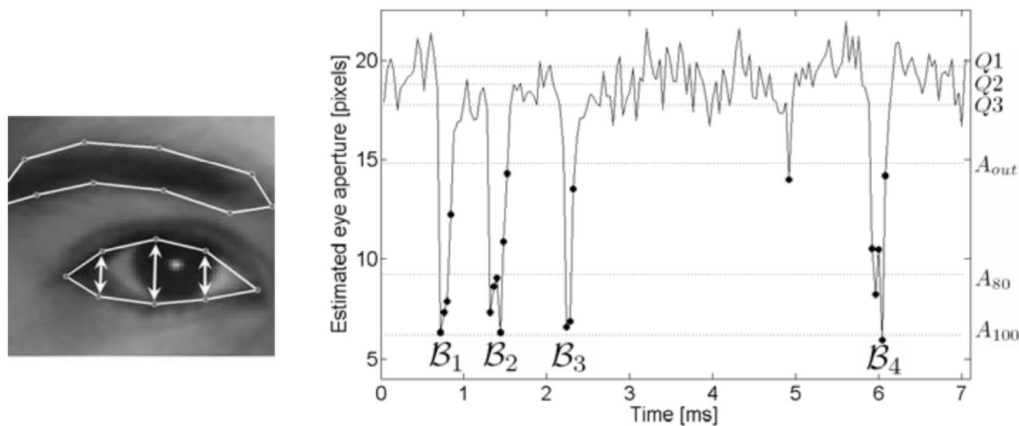


Figure 3.6 Left: the arrows illustrate distances for computing eye aperture $a(t)$. Right: $a(t)$ for several frames with 4 blinks detected. The quartiles Q_1 , Q_2 and Q_3 and values A_0 , A_{80} and A_{100} are depicted. Whole method is described in [20].

are for each of the eye to approximate an eye shape. The aperture $a(t)$ of the eye at time t is computed as average distance between vertically corresponding landmarks. A reference level A_0 is set as a median of $a(t)$. The values $a(t)$ are considered to be outliers if they are lower than heuristic threshold $A_{out} = Q_3 - 1.5(Q_1 - Q_3)$, where Q_1 , Q_2 and Q_3 are quartiles of $a(t)$. The average of peak values of outliers is denoted as A_{100} . They are interested of measuring the PERCLOS [36] metric which is defined as a time that the eyes are closed 80% or more. The threshold denoting that eyes are at least 80% closed is computed as $A_{80} = A_0 - 0.8(A_0 - A_{100})$. The value A_{80} is computed iteratively because some blinks can be discarded or added. The situation is depicted in Fig. 3.6. This approach is suitable only for offline processing because it needs whole video sequence for parameter estimation.

The second system [37] using Active Shape Model is based on eye contour extraction represented by 16 landmarks. Eye openness degree is computed in a similar way as



Figure 3.7 Eye openness degree is computed as a ratio between height of the eyes and a distance between eyes in [37].

we do but a ratio of average height of eyes to a distance between eyes is used, see Fig. 3.7. Eye blink is detected if the eye openness degree changes from larger than threshold $thl = 0.12$ to smaller than $ths = 0.02$. This is a baseline method which do not solve many problems in videos in-the-wild. The method does not admit that the thresholds may be different for different people. It also does not take facial expressions into account. The average time to process one frame is about 140 ms so it runs real-time only for videos with frame rate lower than 7 fps.

The listed methods have different limitations. They are mostly sensitive to image resolution, illumination, or head pose, etc. or their computational cost is high. Many of them do not take into account a fact that it does not generally hold that eye closing always means the eye blinking. We note that many eye blink detectors only distinguish between open and closed states of the eye but they do not detect blinks over time at all.

3.2 Drowsiness detection approaches

One of the most frequent application of blink detection is to detect a subject drowsiness. E.g. it may be used to alert a car driver when he or she is too tired. A standard indicator of drowsiness is PERCLOS [36]: "Proportion of time that the eyes are 80% to 100% closed." Papers [38, 19, 39] estimate drowsiness using PERCLOS. Another common approach is to measure drowsiness according to the blink frequency [40, 41, 39] or according to the blink duration. In [1] blinks are divided according to the duration to 3 groups: *awake* (blink duration shorter than 400 ms), *drowsy* (blink duration between 400 ms and 800 ms) and *sleepy* (blink duration longer than 800 ms). A drowsiness is detected when the eyes remain closed for two or more seconds in [42]. A complex algorithm detecting a subject fatigue is described in [43]. A fatigue is regarded as the result of many variables such as health, sleep history, workload or weather. A Bayesian Network model using together observations such as PERCLOS, percentage of saccade eye movement, eyelid and head movement, etc. is constructed. All parameters used are shown in Fig. 3.8.

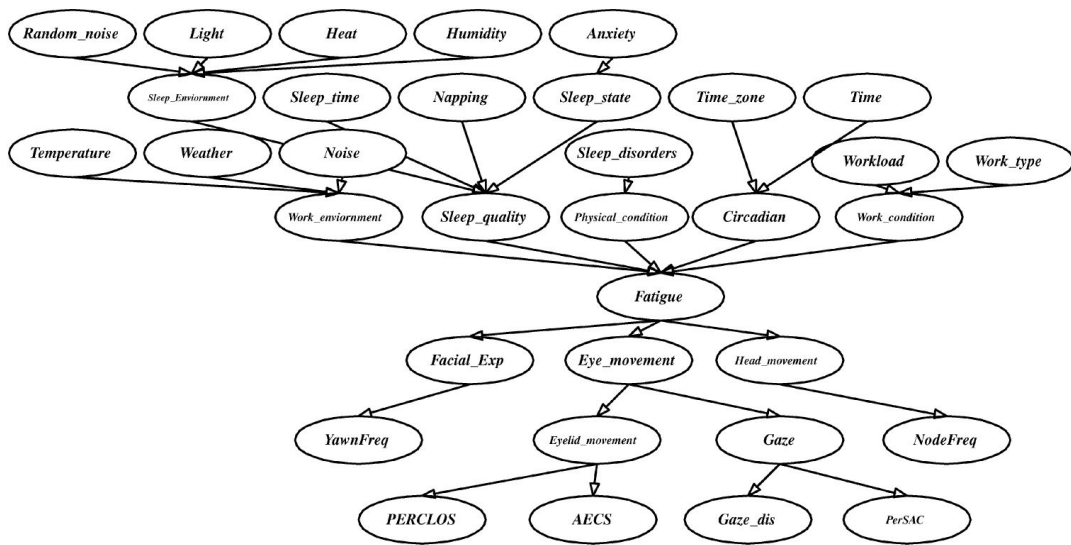


Figure 3.8 A fatigue Bayesian Network model described in paper [43].

4 Proposed method

The eye blink is a fast closing and reopening of a human eye. Each individual has a little bit different pattern of blinks. The pattern differs in the speed of eyelid movement, in a degree of squeezing the eyes and in a blink duration. The eye blink lasts approximately 100-400 ms.

We propose to exploit state-of-the-art facial landmark detectors to localize the eyes and eyelid contours. From the landmarks detected in the image with face, we derive the eye aspect ratio (EAR) that is used as an estimate of the eye openness state. Since the per-frame EAR may not necessarily recognize the eye blinks reliably, a classifier that takes a larger temporal window of a frame into account is trained.

For every video frame, the eye landmarks are detected. The eye aspect ratio (EAR) between height and width of the eye is computed.

$$\text{EAR} = \frac{\|p_2 - p_6\| + \|p_3 - p_5\|}{2\|p_1 - p_4\|}, \quad (4.1)$$

where p_1, \dots, p_6 are the 2D landmark locations, depicted in Fig. 4.1.

The EAR is mostly constant when an eye is open and is getting close to zero while closing the eye. It is partially person and head pose insensitive. Eye aspect ratio of the open eye has a small variance among individuals and it is fully invariant to a uniform scaling of the image and in-plane rotation of the face. Since eye blinking is performed by both eyes synchronously, the EAR of both eyes is averaged. An example of an EAR signal over several frames in the video sequence is shown in Fig. 4.1, 5.8, 5.10, 5.14, 5.15.

Two approaches are proposed in the thesis. The first one is supervised thus training process is needed. An SVM classifier is learned on training dataset. The second method is unsupervised. The blinking is modelled by Hidden Markov Model.

4.1 Eye blink detection using Support Vector Machine classifier (EAR SVM)

It generally does not hold that low value of the EAR means that a person is blinking. A low value of the EAR may occur when a subject closes his/her eyes intentionally for a longer time or performs a facial expression, yawning, etc., or the EAR captures a short random fluctuation of the landmarks.

Therefore, we propose a classifier that takes a larger temporal window of a frame as an input. Due to a normally blink length being from 100 ms to 400 ms, we decided that approximately 430 ms can have a significant impact on a blink detection. Further

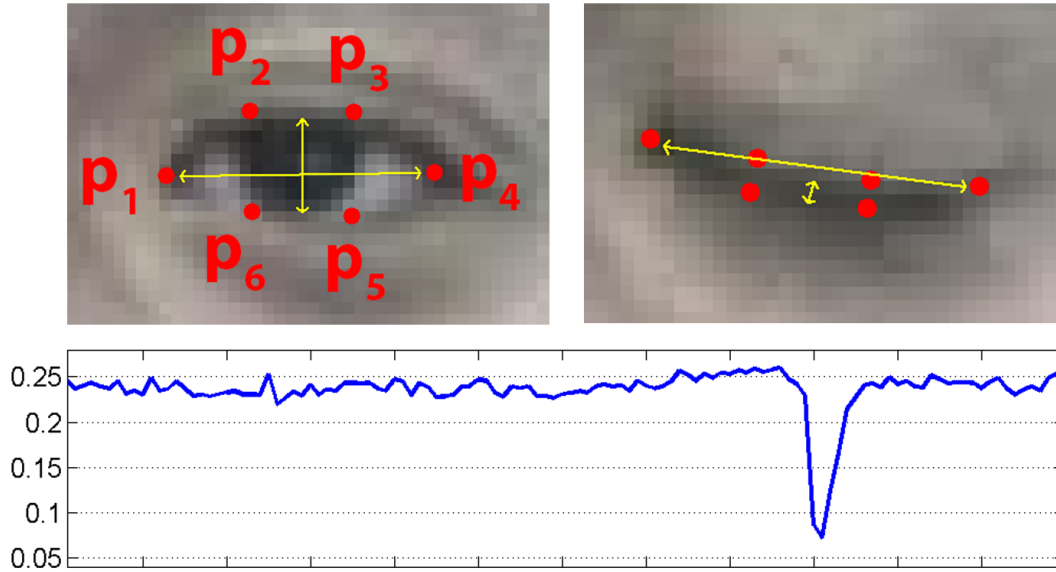


Figure 4.1 Open and closed eyes with landmarks p_i automatically detected by [7]. The eye aspect ratio EAR in Eq. (4.1) plotted for several frames of a video sequence. A single blink is present.

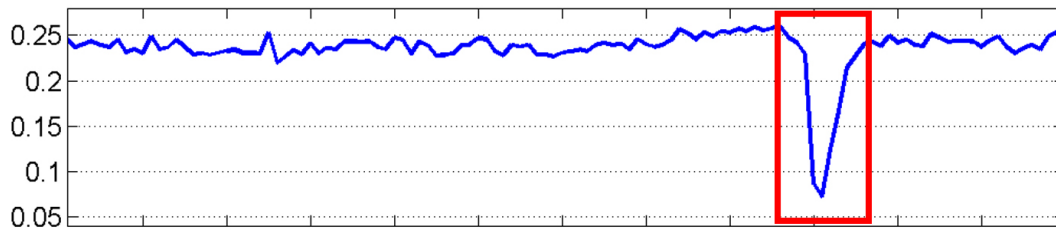


Figure 4.2 The eye aspect ratio EAR in Eq. (4.1) plotted for several frames of a video sequence. A single blink is present. A red box demonstrates the scanning time window.

values are given for 30fps videos. Thus, for example having 30fps video, for each frame a 13-dimensional feature is gathered by concatenating the EARs of its ± 6 neighboring frames, see Fig. 4.2.

A linear SVM classifier (called EAR SVM) is trained from manually annotated sequences. Positive examples are collected as ground-truth blinks, while the negatives are those that are sampled from parts of the videos where no blink occurs, with 5 frames spacing. Additionally, to avoid only eye closing or only eye opening being detected as a positive blink, the starts and ends of the ground-truth blinks are considered as negatives exemplified for training the SVM classifier.

While testing, a classifier is executed in a scanning-window fashion. A 13-dimensional feature is computed and classified by EAR SVM for each frame except the beginning

and ending of a video sequence. The values are proportionately recalculated for different frame rates than 30 fps. Proposed algorithm runs online, it means that the blink is detected immediately after the blink's end.

4.2 Eye blink detection using Hidden Markov Model (EAR adaptive HMM)

The eye blink detection method using SVM described in section 4.1 has several limitations. It is impossible to measure a duration of an eye blink using EAR SVM classifier and it cannot determine longer eye closures. The classifier also needs a lot of heterogeneous annotated data for training. The model is generic which means that it is computed only once and remains the same for all the testing data. The model is not adapted to a specific person. This may result in a failure because blink lengths, closure amplitudes and speed of eyelid movements differ for each individual so the values of EAR over time in Eq. (4.1) are diverse. These characteristics are even non-stationary. It means that they may change over time for a single person. That is the main motivation to use other model which is *adaptive* to a person and time.

We assume that the sequence of observations of the eye aspect ratio values over time is a Markov process where the states of the eye are not directly visible. Thus it is modeled by hidden Markov model (HMM) λ [44, 45, 46]:

$$\lambda = (A, B, \pi) \quad (4.2)$$

where A is the transition matrix, B is the emission matrix and π is the matrix with initial probabilities. The variables A , B and π are described further.

In general for HMM, there are three main problems:

1. The first is the *evaluation* problem. The task is to determine the likelihood of a sequence given the model parameters.
2. The second problem is the *decoding*. The task is to find the most likely sequence of the hidden states generating the observations when the model parameters are known. This problem is solved by Viterbi algorithm [47].
3. The third problem is *learning* the model. The task is to estimate the model parameters that maximize the probability of the observed sequence. This problem is solved Baum-Welch algorithm [44, 46].

The proposed eye blink detection approach using HMM consists of two stages. In the first one it is decided in which of two states eyes are (*open* or *closed* eye states) and in the second stage, the eye blinks are determined according to eye closure length using a simple state machine. Finally, an *adaptation* mechanism to capture the non-stationarity and personalisation is carried out.

4.2.1 Detecting eye states by Hidden Markov Model

The Hidden Markov Model $\lambda = (A, B, \pi)$ is specified by a set of hidden (unobservable) states S . There are only two states in our case. The first state stands for *open* eye and the second for *closed* eye:

$$S = \{s_1, s_2\} = \{open, closed\} \quad (4.3)$$

We have a state sequence Q of length T which is a number of frames in a video sequence:

$$Q = \{q_1, q_2, \dots, q_T\}. \quad (4.4)$$

and corresponding observation sequence O :

$$O = \{o_1, o_2, \dots, o_T\}, \quad (4.5)$$

the observations o_t are directly the values of EAR (4.1) for each frame. The initial probabilities of states are determined by matrix $\pi = [\pi_i]$, where:

$$\pi_i = P(q_1 = s_i), \quad (4.6)$$

for states $i \in \{1, 2\}$. The model is also described by a time independent transition matrix $A = [a_{ij}]$ which stores the probabilities of one state being followed by another state:

$$a_{ij} = P(q_t = s_j | q_{t-1} = s_i) \quad (4.7)$$

for $i \in \{1, 2\}$, $j \in \{1, 2\}$ and $t \in \{2, \dots, T\}$. The emissions $B = [b_i(o_t)]$ describe the probability of a particular observation o_t at time t for state i :

$$b_i(o_t) = p(o_t | q_t = s_i) \quad (4.8)$$

for $i \in \{1, 2\}$ and $t \in \{1, \dots, T\}$. The emission probabilities B can be either discrete or continuous. It is more advantageous to use continuous emissions for our purpose. We suppose that the observation o_t for *open* and *closed* eye can be modeled by the Gaussian model:

$$b_i(o_t) = \mathcal{N}(\mu_i, \sigma_i^2) \quad (4.9)$$

for $i \in \{1, 2\}$ and $t \in \{1, \dots, T\}$, with mean values μ_i , and variance σ_i^2 .

HMM parameters need to be estimated. These are transition matrix A between states, prior probabilities of states π and two means and standard deviations to get emission probabilities B in Fig. 4.3 modeled by Gaussian distributions. The parameters are learned in an unsupervised fashion by observing a short sequence of EAR values. This is estimated by Baum-Welch algorithm which is in fact a kind of Expectation Maximization algorithm [48]. Maximum likelihood estimate is found by a local iterative algorithm. An initialization is therefore needed. Having learned the model parameters, the hidden states are estimated for each video frame by Viterbi [47] algorithm using the dynamic programming to find the highest score over the sequence.

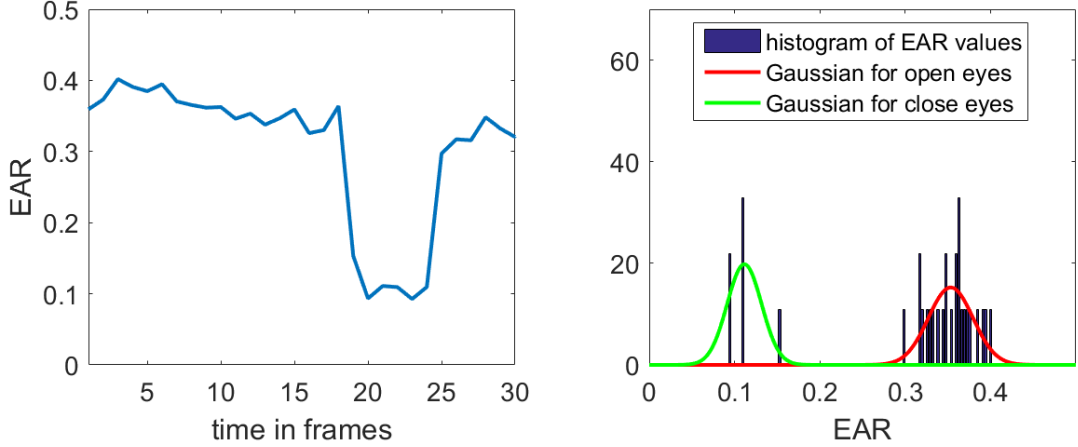


Figure 4.3 There are EAR values from Eq. (4.1) plotted for several frames of a video sequence by blue line with a single blink present (left). The corresponding normalized histogram of EARs. Green and red lines show fitted Gaussians (right).

4.2.2 Detecting blinks via state machine

The algorithm proposed in 4.2.1 only distinguishes between open and closed eyes. Once the eye states are estimated the eye blinks are detected by a simple state machine which decides if the eye closure detected by the HMM is eye blinking according to the length of the closure. The average eye blink duration is between 60 ms to 700 ms according to the annotated datasets. Thus we consider closures of length between 60 ms and 700 ms being blinks.

4.2.3 Adaptation of HMM in time

The testing process is initialized with a generic model parameters learned from an annotated training dataset with ground-truth. The generic transition matrix is determined by relative frequencies and Gaussian distributions are fitted having the blink/non-blink labels. The generic model parameters are the same for all the testing videos and are learned only once. They are used only for the initialization of a model of each tested sequence and further the algorithm using adaptation is unsupervised. The parameters of the HMM are then repeatedly reestimated in time intervals I to adapt the model to a specific person. Subsequent model estimation is initialized by the previous solution. For new estimation only the subsequence of size S of the EAR values is used as an input for Baum-Welch algorithm.

The current parameters are then computed as a convex combination of several last estimates with exponential weights w_t . Thus more recent estimates have higher weights. The weights are normalized to sum up to one. The estimates older than learning time L are forgotten:

$$w_t = \frac{e^{\frac{t}{L}}}{\sum_{t=1}^L e^{\frac{t}{L}}}, \quad (4.10)$$

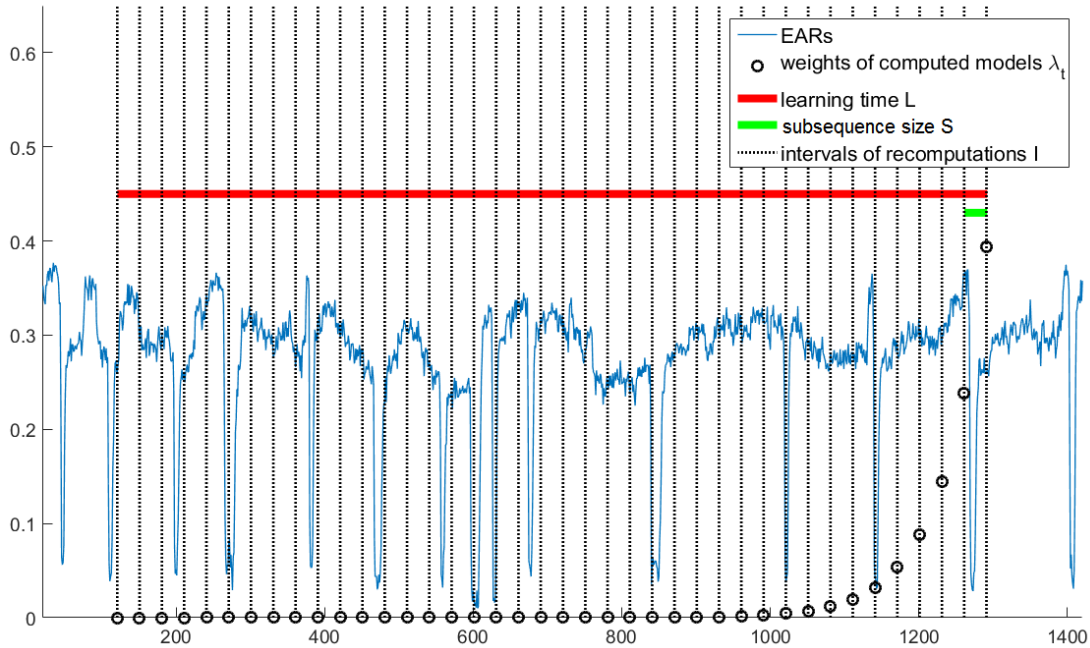


Figure 4.4 The eye aspect ratio EAR in Eq. (4.1) plotted for several frames of a video sequence by blue line. The black points show the weights w_t of models estimated in time t . Red line is the time L of remembering previous models. Green line shows the size of subsequence S of EARs used for computation of new model and dotted black lines show intervals I how often the new model is computed.

where $t = 1, \dots, \frac{L}{I}$. Therefore the parameters of the HMM are iteratively adapting to be person and time period specific. Between intervals of reestimations of the parameters, the last calculated model for decoding is used.

The subsequence size S must be large enough to include whole blink plus some surroundings and simultaneously it must be small enough to quickly adapt the model to a change and do not make mistake on transitions, e.g. when a subject starts squeezing its eyes while smiling or when an illumination condition has changed. The time interval I of model reestimations must be long enough to be able to capture the non-stationarity. The situation is depicted in Fig. 4.4.

The parameters of the model are not recomputed in a case that no eye state change is present. It is recognized heuristically by the difference between the lowest and the highest value of the EAR in the subsequence. The difference is not higher than threshold D . If this happens, we do not reestimate whole the model by Baum-Welch algorithm. We only fit one Gaussian distribution. Due to the mean of the Gaussian we determine if it belongs to *open* or *closed* eye state. To complete the model λ_t at time t the generic values are used for the second Gaussian distribution and the rest of the hidden Markov model parameters remains the same.

5 Experiments and datasets

Two types of experiments were carried out: the experiments that measure accuracy of the landmark detectors, see Sec. 5.1, and the experiments that evaluate performance of the whole eye blink detection algorithms, see Sec 5.2.

5.1 Accuracy of landmark detectors

To evaluate accuracy of tested landmark detectors, we used the 300-VW dataset [49]. It is a dataset containing 50 videos where each frame has associated a precise annotation of facial landmarks. The videos are “in-the-wild”, mostly recorded from a TV.

The purpose of the following tests is to demonstrate that recent landmark detectors are particularly robust and precise in detecting eyes, i.e. the eye-corners and contour of the eyelids. Therefore we prepared a dataset, a subset of the 300-VW, containing sample images with both open and closed eyes. More precisely, having the ground-truth landmark annotation, we sorted the frames of each of the 50 videos by the eye aspect ratio (EAR in Eq. (4.1)) and took 10 frames of the highest ratio (eyes wide open), 10 frames of the lowest ratio (mostly eyes tightly shut) and 10 frames sampled randomly. This way we collected 1500 images. Moreover, all the images were later subsampled (successively 10 times by factor 0.75) in order to evaluate accuracy of tested detectors on small face images.

Two state-of-the-art landmark detectors were tested: Chehra [7] and Intraface [6]. Both run in real-time¹. Samples from the dataset are shown in Fig. 5.1. Notice that faces are not always frontal to the camera, the expression is not always neutral, people are often speaking emotionally or smiling, etc. Sometimes people wear glasses or hair may occasionally partially occlude one of the eyes. Both detectors perform generally well, but the Intraface is more robust to very small face images, sometimes at impressive extent as shown in Fig. 5.1.

Quantitatively, the accuracy of the landmark detection for a face image is measured by the average relative landmark localization error, defined as usually

$$\epsilon = \frac{100}{\xi N} \sum_{i=1}^N \|x_i - \hat{x}_i\|_2, \quad (5.1)$$

where x_i is the ground-truth location of landmark i in the image, \hat{x}_i is an estimated landmark location provided by a detector, N is a number of landmarks and normalization factor ξ is the inter-ocular distance (IOD), i.e. Euclidean distance between eye centers in the image.

¹Intraface runs in 50 Hz on a standard laptop.

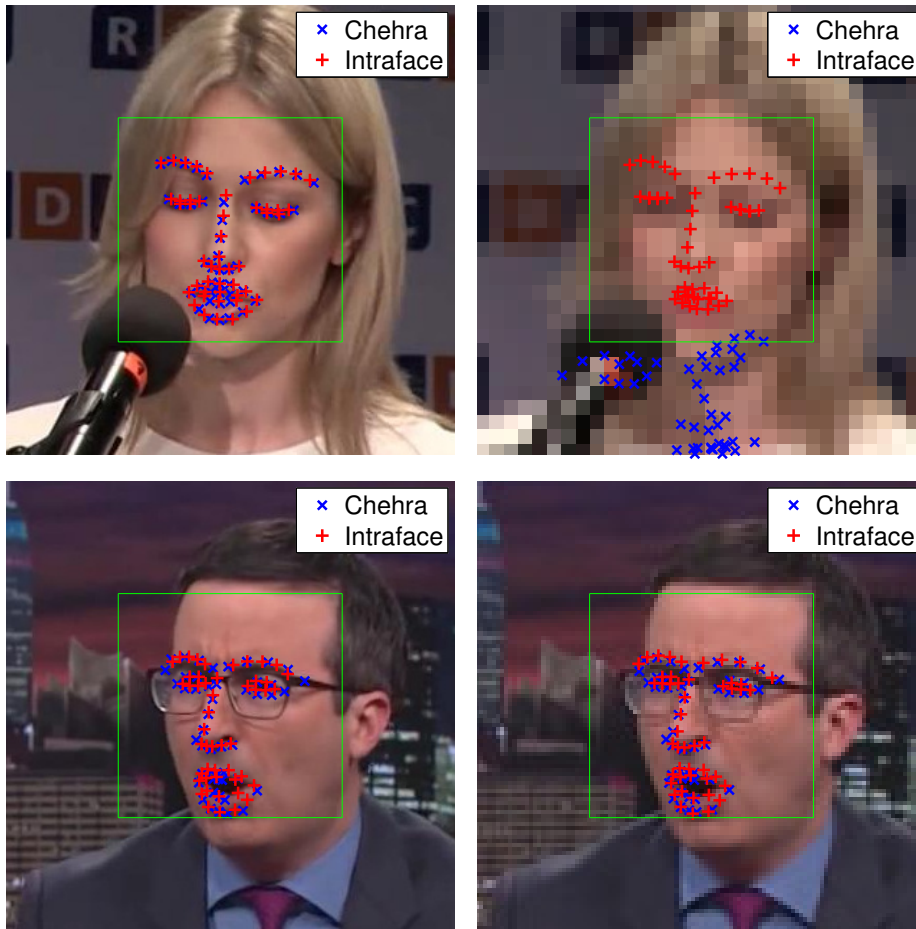


Figure 5.1 Example images from the 300-VW dataset with landmarks obtained by Chehra [7] and Intraface [6]. Original images (left) with inter-ocular distance (IOD) equal to 63 (top) and 53 (bottom) pixels. Images subsampled (right) to IOD equal to 6.3 (top) and 17 (bottom).

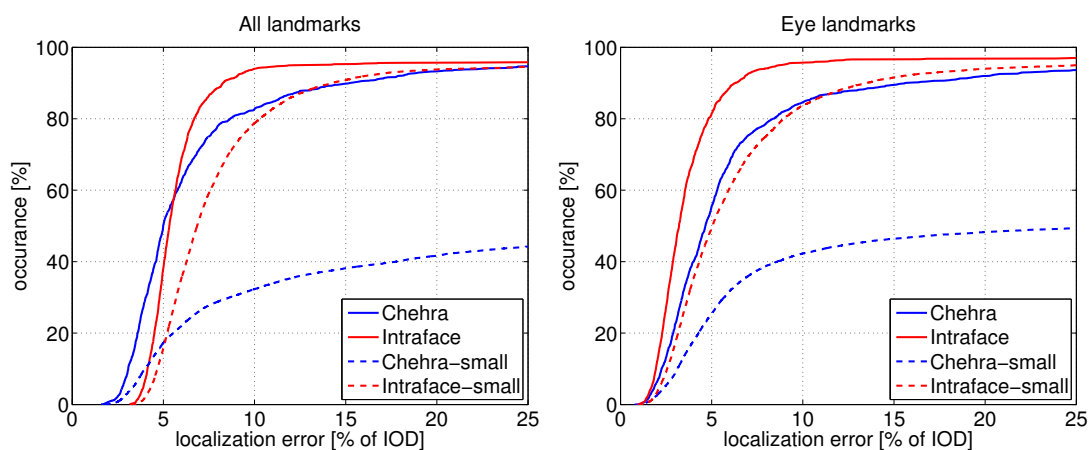


Figure 5.2 Cumulative histogram of average localization error of all 49 landmarks (left) and 12 landmarks of the eyes (right). The histograms are computed for original resolution images (solid lines) and a subset of small images (IOD \leq 50 px).

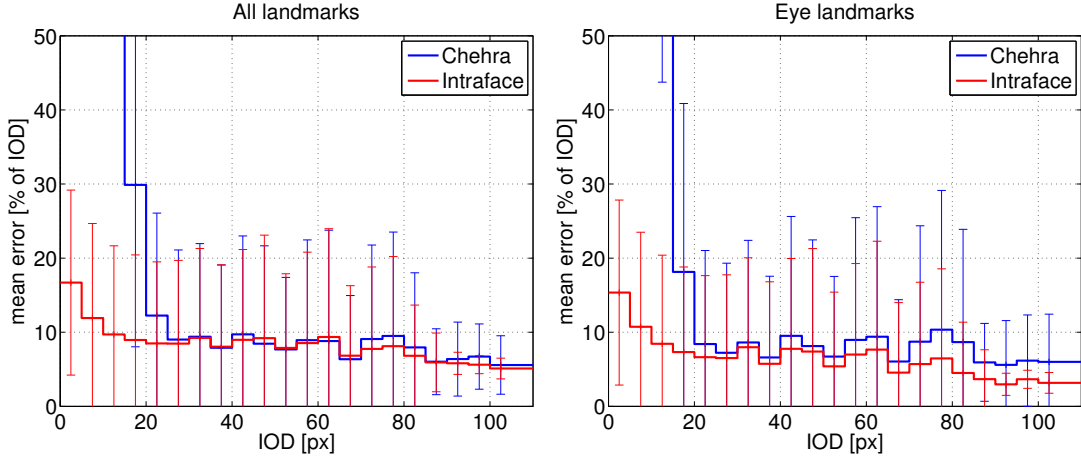


Figure 5.3 Landmark localization accuracy as a function of the face image resolution computed for all landmarks and eye landmarks only.

First, a standard cumulative histogram of the average relative landmark localization error ϵ was calculated, see Fig. 5.2, for a complete set of 49 landmarks and also for a subset of 12 landmarks of the eyes only, since these landmarks are used in the proposed eye blink detector. The results are calculated for all the original images that have average IOD around 80 px, and also for all “small” face images (including subsampled ones) having $\text{IOD} \leq 50$ px. For all landmarks, Chehra has more occurrences of very small errors (up to 5 percent of the IOD), but Intraface is more robust having more occurrences of errors below 10 percent of the IOD. For eye landmarks only, the Intraface is always more precise than Chehra. As already mentioned, the Intraface is much more robust to small images than Chehra. This behaviour is further observed in the following experiment.

Taking a set of all images, we measured a mean localization error μ as a function of a face image resolution determined by the IOD. More precisely,

$$\mu = \frac{1}{|\mathcal{S}|} \sum_{j \in \mathcal{S}} \epsilon_j, \quad (5.2)$$

i.e. average error over set of face images \mathcal{S} having the IOD in a given range. Results are shown in Fig. 5.3. Plots have errorbars of standard deviation. It is seen that Chehra fails quickly for images with $\text{IOD} < 20$ px. For larger faces, the mean error is comparable, although slightly better for Intraface for the eye landmarks.

The last test is directly related to the eye blink detector. We measured accuracy of EAR as a function of the IOD. Mean EAR error is defined as a mean absolute difference between the true and the estimated EAR. The plots in Fig. 5.4 are computed for two subsets: closed/closing (average true ratio 0.05 ± 0.05) and open eyes (average true ratio 0.4 ± 0.1). The error is higher for closed eyes. The reason is probably that both detectors are more likely to output open eyes in case of a failure. It is seen that eye aspect ratio error for $\text{IOD} < 20$ px causes a major confusion between open/closed eye

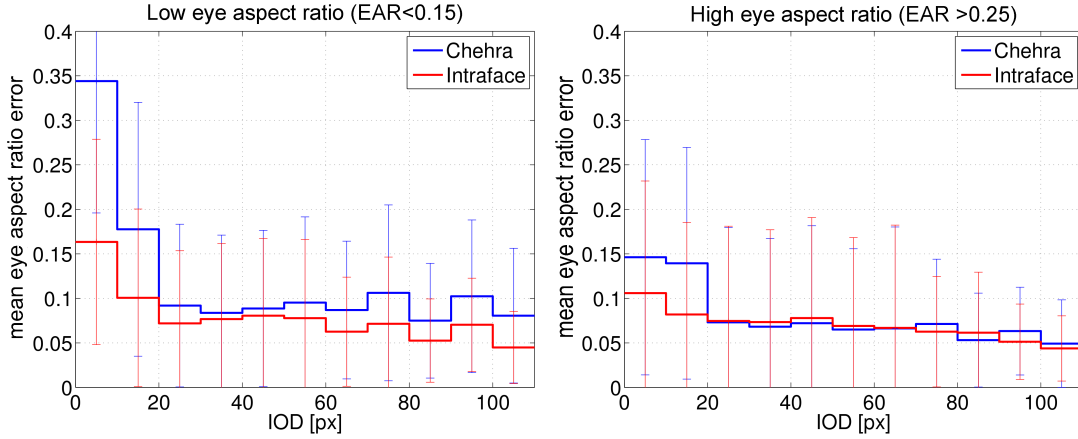


Figure 5.4 Accuracy of the EAR as a function of the face image resolution. Left: for images with small true ratio (mostly closing/closed eyes), and right: images with higher ratio (open eyes).

states for Chehra, nevertheless for larger faces the ratio is estimated precisely enough to ensure a reliable eye blink detection.

5.2 Eye blink detector evaluation

The substantial experiment of the thesis evaluates the proposed blink detectors. Firstly the available eye blink datasets are presented in 5.2.1. Then the error rates of the eye blink detectors are detailed and finally experiments on robustness against face resolution and frame rate are carried out.

As a result of the study measuring the accuracy of landmark detectors in Sec. 5.1, we decided to use only Intraface [6] landmarks for computation of EAR in Eq. (4.1) in further experiments due to its excellent performance.

The proposed SVM and HMM based detectors are compared, together with a baseline method of thresholding of EAR values. The results are reported in Subsec. 5.2.2 and Subsec. 5.2.3.

There is no standard unified method for measuring accuracy of the eye blink detectors so the comparison with other methods [3, 23, 1] is only illustrative. We evaluate it following Fogelton and Benesova [35].

We use an intersection over union overlap

$$IOU = \frac{intersection}{union} \quad (5.3)$$

to measure an overlap between the ground-truth and detected blink intervals, see Fig. 5.5. Pairs of the ground-truth and detected blinks having an overlap over 20 percent are found. These pairs are sorted by its IOU overlap. Then we take the pairs in decreasing order of IOU and iteratively match the unmatched pairs of blinks with the highest score of IOU. Pairs where at least one blink is already matched are not considered anymore. Finally, a number of matched pairs is a number of true positives.

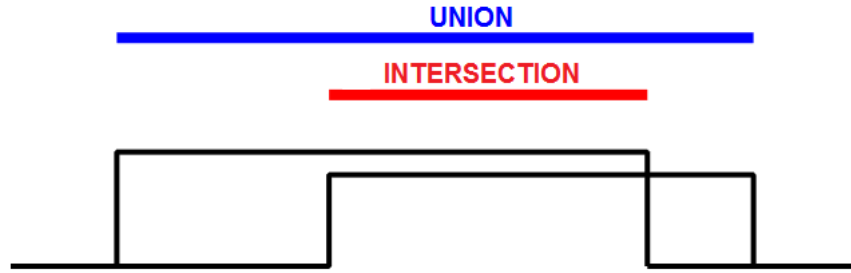


Figure 5.5 Intersection over union overlap of ground-truth blink with detected blink.

Unmatched ground-truth blinks are false negatives and unmatched detected blinks are false positives. So each ground-truth as well as each detected blink is counted only once.

5.2.1 Datasets for blink detection

We evaluate on three standard datasets with ground-truth annotations of blinks. The annotations were normalized to have each blink annotated with its starting and ending frame.

ZJU

The ZJU [5] dataset is consisting of 80 short videos of 20 subjects. Each subject has 4 videos: 2 with and 2 without glasses, 3 videos are frontal and 1 is an upward view. The 30fps videos are of size 320×240 px. An average video length is 136 frames and contains about 3.6 blinks in average. An average IOD is 57.4 pixels. In this database, subjects do not perform any noticeable facial expressions. They look straight into the camera at close distance, almost do not move, do not either smile nor speak. A ground-truth blink is defined by its beginning frame, peak frame and ending frame. Examples of video frames are shown in Fig. 5.6.

Eyeblink8

The dataset Eyeblink8 [3] is more challenging. It consists of 8 long videos of 4 subjects that are smiling, rotating head naturally, covering face with hands, yawning, drinking and looking down probably on a keyboard. These videos have length from 5k to 11k frames, also 30fps, with a resolution 640×480 pixels and an average IOD 62.9 pixels. They contain about 50 blinks on average per video. Each frame belonging to a blink is annotated by half-open or close state of the eyes. We consider half blinks, which do not achieve the close state, as full blinks to be consistent with the other datasets. Examples of video frames are shown in Fig. 5.7.



Figure 5.6 Examples of frames of the ZJU dataset [5].



Figure 5.7 Examples of frames of the Eyeblick8 dataset [3].

The Silesian eye blink dataset

The Silesian dataset [50, 34] is recorded in 100 fps in a resolution of 640×480 pixels. It consists of 5 videos of men at close distance in front of the camera. The average IOD is 146.7 pixels. The scene is very simple. The subjects almost do not move and they are recorded from frontal position all the sequence. Each video lasts about two minutes, more accurately they have length from 8k to 16k frames. There are 56 blinks on average per video sequence.

5.2.2 EAR SVM eye blink detector

The eye blink detector based on SVM is detailed in Sec. 4.1. The SVM classifier uses a 13-dimensional features for all frame rates. Therefore time windows must be interpolated to be 13-dimensional for different frame rates than 30 fps. The experiment with EAR SVM is done in a cross-dataset fashion using all the three blink datasets. E.g. it means that the SVM classifier is trained on the Eyeblick8 [3] and ZJU [5] and tested ¹ on the Silesian [50, 34] and all three combinations are alternated. The testing is done using sliding window with a step of a single frame.

Besides testing the proposed EAR SVM method, that is trained to detect the specific blink pattern, we compare with a simple baseline method, EAR thresholding, which only thresholds the EAR in Eq. (4.1) values. The precision-recall curves shown in Fig. 5.9 of the EAR thresholding and EAR SVM classifier were calculated by spanning a threshold of the EAR and SVM output score respectively. Notice, the precision-recall curves are not monotonic due to the matching between the ground-truth and detection blinks involved in the evaluation, see introduction in Sec. 5.2. So it does not hold that

¹The EAR SVM detector evaluates only frames in the middle of a blink as positives but we need to have positive detection during the whole blink because of evaluating using overlap with the ground-truth. Thus we need to extend the detected blinks by ± 100 ms (± 3 frames while having 30fps videos) to obtain a longer pulse of a detected blink.

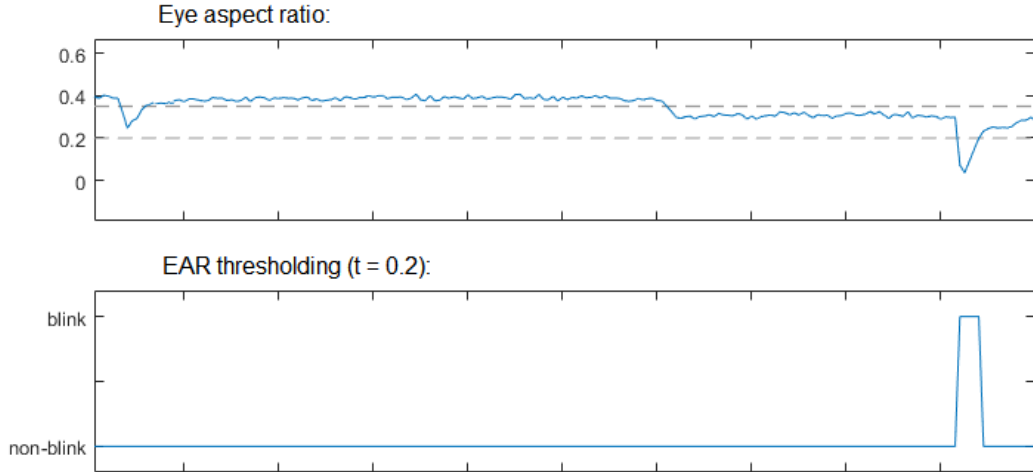


Figure 5.8 An example pointing to how difficult is to set a correct threshold while thresholding the EAR curve. If the threshold is set to 0.35 the left blink will be detected but in right half of a plot there would be long false positive. If the threshold is set to 0.2 then the right blink is detected but the left blink is missed.

with increasing recall it decreases precision and vice versa. For easier comparison the operational points with the highest F_1 score (5.4) were extracted from the precision-recall curves and published in Tab. 5.1.

$$F_1 = 2 \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}} \quad (5.4)$$

It is very difficult to estimate a correct threshold convenient for all the video sequences, see example in Fig. 5.8. So the thresholding method makes many mistakes. The proposed EAR SVM detector outperforms the methods by Drutarovsky and Fogelton [3], Lee et al. [23] and Danisman et al. [1]. The method by Fogelton and Benesova [35] is comparable with ours for Eyeblink8 and Silesian datasets. But we slightly lag behind the method by Fogelton and Benesova [35] at the ZJU dataset. We have counted more false negatives. However, we believe that this is mostly caused by the fact that the videos from ZJU frequently start or end during the blink and a whole blink time window is needed for EAR SVM classification. The results of the other methods are depicted with our precision-recall curves in Fig. 5.9.

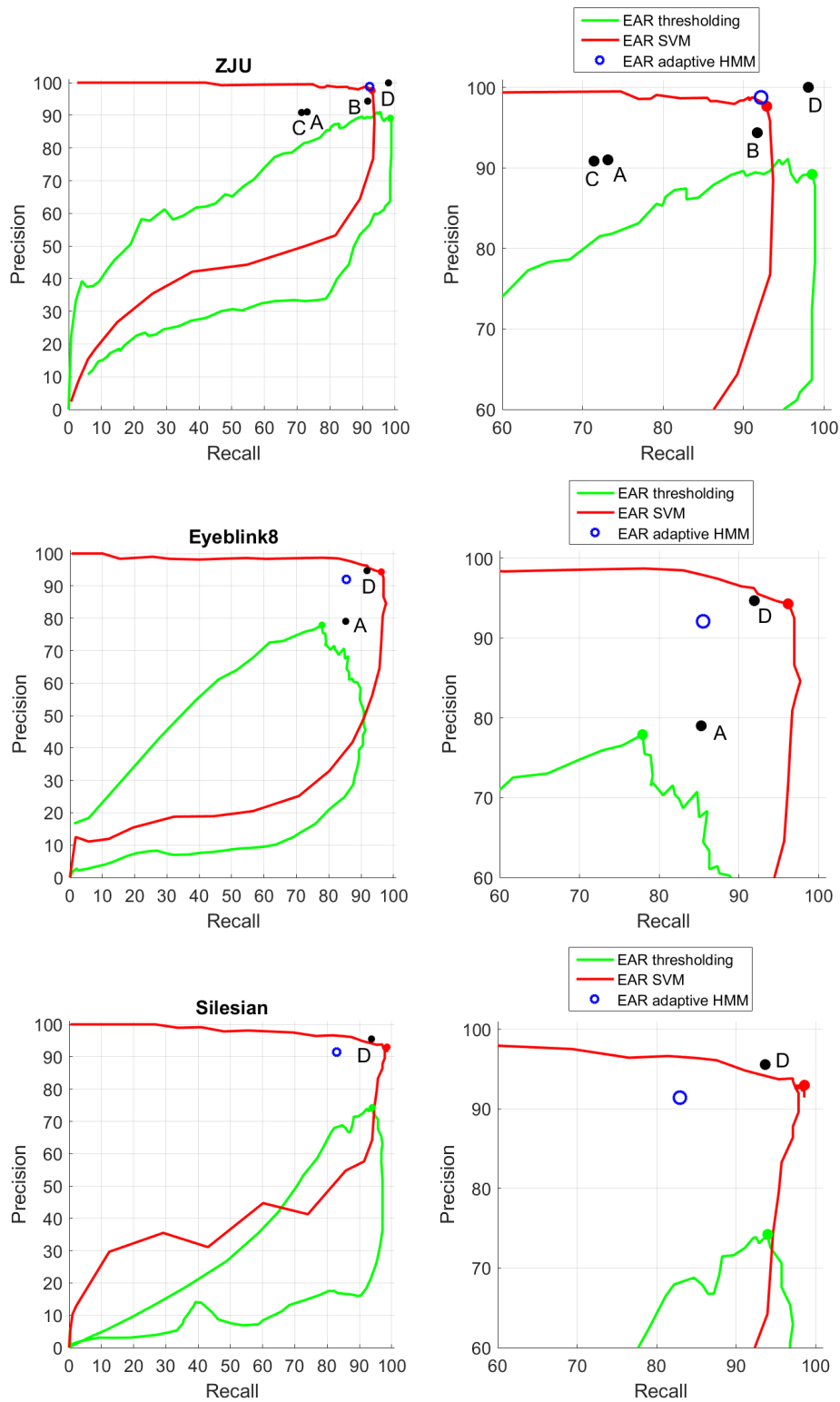


Figure 5.9 Precision-recall curves of the EAR thresholding, EAR SVM and EAR adaptive HMM classifiers measured on the ZJU (top row), the Eyblink8 (middle row) and the Silesian (bottom row) datasets. The operational points with the highest F_1 score (5.4) for thresholding (resp. SVM) method are drawn by green (resp. red) points. Published results of methods A - Drutarovsky and Fogelton [3], B - Lee et al. [23], C - Danisman et al. [1], D - Fogelton and Benesova [35] are depicted. Plots in the right column are zoomed to those on the left.

5.2.3 EAR adaptive HMM eye blink detector

The EAR adaptive HMM method and its parameters are detailed in Sec. 4.2. The generic parameters of the HMM are learned using the ground-truth annotation from datasets ZJU and Eyeblick8. The first state is *open* eye and the second state is *closed* eye. The generic transition matrix is set:

$$A_G = \begin{bmatrix} 0.99 & 0.01 \\ 0.11 & 0.89 \end{bmatrix}, \quad (5.5)$$

generic initial probabilities are:

$$\pi_G = \begin{bmatrix} 0.98 & 0.08 \end{bmatrix} \quad (5.6)$$

generic means for open and close state are determined as:

$$\mu_G = \begin{bmatrix} 0.3 & 0.11 \end{bmatrix} \quad (5.7)$$

and generic standard deviations:

$$\sigma_G = \begin{bmatrix} 0.06 & 0.04 \end{bmatrix}. \quad (5.8)$$

The parameters for adaptation of the model are set experimentally. Older models than the learning time:

$$L = 40s \quad (5.9)$$

are forgotten. The subsequence size of the time window used for learning new model parameters is:

$$S = 1s, \quad (5.10)$$

the interval of recomputation of a new model is:

$$I = 1s, \quad (5.11)$$

and the threshold:

$$D = 0.15, \quad (5.12)$$

which is described in Subsec. 4.2.3. An interpretation of the parameters is illustrated in Fig. 4.4.

The results of eye blink detection of EAR adaptive HMM method are depicted in Fig. 5.9 together with the results of EAR SVM and EAR thresholding. We can see that the EAR adaptive HMM has better results in a comparison with the baseline method of EAR thresholding on all the three datasets. But apart from the ZJU dataset the unsupervised EAR adaptive HMM classifier is a little bit worse compared with the supervised EAR SVM method. Some of the errors of the EAR adaptive HMM method are caused by slow adaptation of the model. If a person-specific model vary

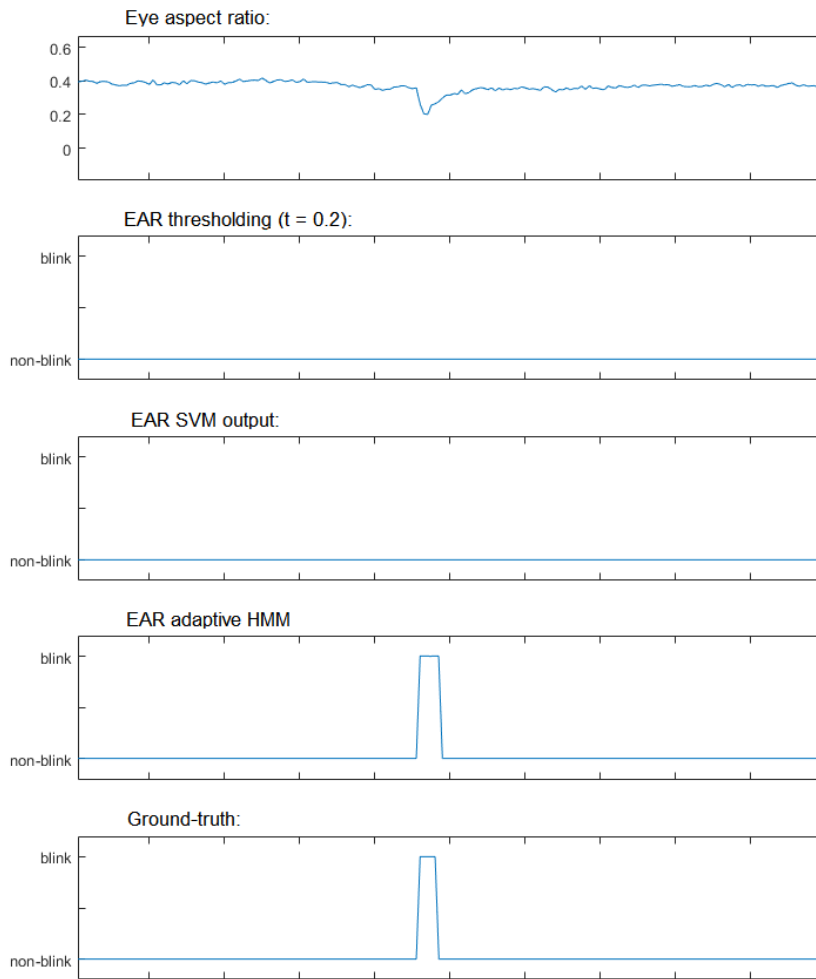


Figure 5.10 An example of a weak blink. Only the EAR adaptive HMM method correctly detects the blink.

	ZJU			Eyeblick8			Silesian		
	thr.	SVM	HMM	thr.	SVM	HMM	thr.	SVM	HMM
precision	89.2	97.7	98.8	77.9	94.3	92.1	74.2	93.0	91.4
recall	98.5	92.9	92.2	77.9	96.2	85.5	94.0	98.6	82.9
threshold	0.27	1.2	-	0.08	0.2	-	0.15	0.4	-

Table 5.1 The operational points having the highest F_1 score (5.4) from all points in precision-recall curves of thresholding and EAR SVM method. The result of EAR adaptive HMM for three standard datasets.

a lot from the generic one or a person squints its eyes by smiling for example, it lasts some time to adapt the model parameters. Another part of the error of the HMM based method rises on the transition between open and half-open eyes. When a subject squints his/her eyes, but does not close the eyes fully, the system firstly detects the half-open eyes as closed and then it adapts to consider them as open. So the eyes are detected as closed only at the beginning of eyes squeezing. The symmetric situation happens at the end of eye squeezing. Nevertheless, there are multiple situations where EAR adaptive HMM method is better than EAR SVM, for example when a blink is not very dominant. In Fig. 5.10 the blink impulse is very weak and all the methods fail except the EAR adaptive HMM.

An important advantage of the eye blink detector using hidden Markov model is that it can distinguish between open and close states even out of blinking. Besides computing a frequency of blinking it is thus capable to determine a duration of a particular eye closure and so it can measure the total time of eyes being closed. This can be very useful to detect a subject's drowsiness which is reflected in the eye blink duration and frequency.

5.2.4 Computation of blink statistics

The main blink properties are blink frequency, duration, amplitude and a speed of eyelid movement while closing or opening the eye. We measure blink frequency, duration and amplitude at this experiment.

Blink frequency

Firstly a number of detected blinks N_D is compared with a number of ground-truth blinks N_{GT} . Then the frequencies of detected F_D and ground-truth F_{GT} blinks are compared. We use a number of blinks per minute unit. The statistics are listed in Tab. 5.2 for each video of Eyeblink8 and Silesian datasets. Because the ZJU dataset contains 80 videos, we do not show results of each video separately but only for the whole dataset. The average blink frequency is 17 blinks per min, during conversation it increase to 26 and it decreases to 5 blinks per minute while reading according to the literature [51]. Based on these assumptions we can suspect that people are more concentrated in Eyeblink8. There is a little above average blink frequency at Silesian although they are not talking. But at ZJU the blink frequency about 45 blinks per minute is really abnormal. We believe that the subjects are not blinking spontaneously and they were informed that they were recorded for the purpose of a blink study.

Blink duration

The important property of blinking besides frequency is blink duration. Every person has a little bit different length of an average blink and it can also reflect a person's drowsiness and mood. We are unable to measure a blink duration using EAR SVM

Eyeblick8

Video name	N_{GT}	N_D	N_D	F_{GT}	F_D	F_D	Err SVM [%]	Err HMM [%]
		SVM	HMM	[#b/min]	SVM	HMM		
Eyeblick8 1	30	32	24	4.8	5.2	3.9	+6.6	-20.0
Eyeblick8 2	88	88	73	14.4	14.4	11.9	0.0	-17.1
Eyeblick8 3	61	57	66	11.9	11.6	12.9	-6.5	+8.2
Eyeblick8 4	31	31	32	10.6	10.6	11.0	0.0	+3.2
Eyeblick8 5	73	73	66	14.7	14.7	13.3	0.0	-9.6
Eyeblick8 6	43	42	36	16.4	15.8	13.5	-2.3	-16.3
Eyeblick8 7	29	33	34	4.9	5.6	5.8	+13.8	+17.3
Eyeblick8 8	39	42	35	14.3	15.4	12.9	+7.7	-10.3
All videos	394	398	366	10.8	10.9	10.0	+1.0	-7.1

Silesian

Video name	N_{GT}	N_D	N_D	F_{GT}	F_D	F_D	Err SVM [%]	Err HMM [%]
		SVM	HMM	[#b/min]	SVM	HMM		
Silesian 1	88	90	69	45.9	47.0	36.0	+2.3	-21.6
Silesian 2	31	38	35	11.6	14.2	13.1	+22.6	+12.9
Silesian 3	54	57	49	31.7	33.5	28.8	+5.6	-9.3
Silesian 4	77	80	70	35.1	36.4	31.9	+3.9	-9.1
Silesian 5	31	33	32	22.9	24.4	23.6	+6.5	+3.2
All videos	281	298	255	28.6	30.3	25.9	+5.0	-9.2

ZJU

	N_{GT}	N_D	N_D	F_{GT}	F_D	F_D	Err SVM [%]	Err HMM [%]
		SVM	HMM	[#b/min]	SVM	HMM		
All videos	269	262	251	44.5	43.4	41.5	-2.6	-9.3

Table 5.2 Blink frequencies of Eyeblick8, Silesian and ZJU datasets. N_{GT} is a number of ground-truth blinks, N_D is a number of detected blinks either by EAR SVM method or by method using EAR adaptive HMM. F_{GT} (resp. F_D) is an average number of ground-truth blinks (resp. detected blinks either by SVM or HMM) per one minute. The last two columns show error in percent.

Eyeblink8

Video name	μ_{GT}	μ_D	Err μ	σ_{GT}	σ_D	Err σ	Closed eyes [%]
Eyeblink8 1	371	274	-98	273	156	-117	6.3
Eyeblink8 2	437	349	-87	167	120	-47	9.7
Eyeblink8 3	307	271	-36	95	118	+23	7.0
Eyeblink8 4	352	273	-79	146	117	-30	5.5
Eyeblink8 5	272	243	-29	78	122	+44	11.2
Eyeblink8 6	262	297	+35	103	164	+62	17.4
Eyeblink8 7	300	250	-50	64	109	+46	8.2
Eyeblink8 8	375	254	-121	182	109	-73	12.3
All videos	339	281	-58	157	130	-27	9.1

Silesian

Video name	μ_{GT}	μ_D	Err μ	σ_{GT}	σ_D	Err σ	Closed eyes [%]
Silesian 1	365	297	-69	101	167	+66	27.9
Silesian 2	294	265	-28	63	164	+101	10.7
Silesian 3	378	227	-151	183	152	-31	22.0
Silesian 4	345	245	-100	74	114	+40	22.5
Silesian 5	368	209	-159	109	93	-15	9.4
All videos	354	254	-101	115	145	+30	18.5

ZJU

	μ_{GT}	μ_D	Err μ	σ_{GT}	σ_D	Err σ	Closed eyes [%]
All videos	262	187	-75	105	94	-11	13.2

Table 5.3 Blink duration statistics of Eyeblink8, Silesian and ZJU datasets measured with the EAR adaptive HMM method proposed in Subsec. 5.2.3. The first three columns show mean values in milliseconds of duration of blinks according to ground-truth μ_{GT} and detected μ_D blinks. The error is computed as a difference of means. Next three columns show standard deviations in milliseconds. The last column is a total time in percent of being eyes in the closed state.

$\min y_{max}$	$\max y_{max}$	μy_{max}	σy_{max}
0.11	0.42	0.29	0.06

Table 5.4 Minimal, maximal, mean and standard deviation from average y_{max} from all videos.

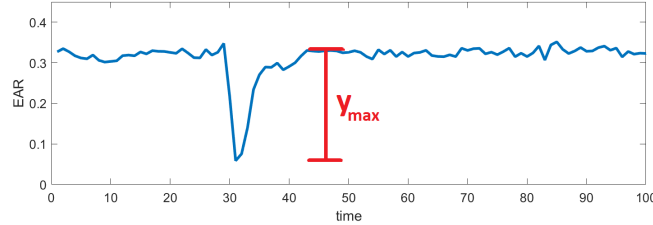


Figure 5.11 The blink amplitude y_{max} .

classifier because it detects only peak of an eye blink. Therefore we must use the EAR adaptive HMM method proposed in Subsec. 5.2.3. This method defines blinks as eye closure longer than 60 ms and shorter than 700 ms. The following experiment measures eye blink duration and estimates a total time of eyes being in a closed state.

From results depicted in Tab. 5.3 we can see that the average blink length is about 250 milliseconds. The detected mean values and standard deviations of blink duration are compared with the ground-truth. However, we note that the annotation of blinks is of a limited precision. It is very subjective and tedious to delineate the start and end of a single blink precisely and including at Silesian dataset which is recorded at a higher frame rate of 100 fps.

Blink amplitude

Another interesting blink statistics is a blink amplitude y_{max} which describes the degree of openness. It differs between people and it also depends on head pose. The blink amplitude is the mean difference between EAR at open state and at closed state, see Fig. 5.11. The purpose of this experiment is to show that blink amplitudes vary a lot.

For each video we measured average maximal amplitude y_{max} while blinking. Then we have computed minimal, maximal, mean and standard deviation from y_{max} from all videos in Tab. 5.4. The histogram of y_{max} values is shown in Fig. 5.12.

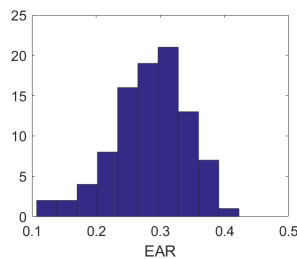


Figure 5.12 The histogram of average amplitude y_{max} calculated for each video.

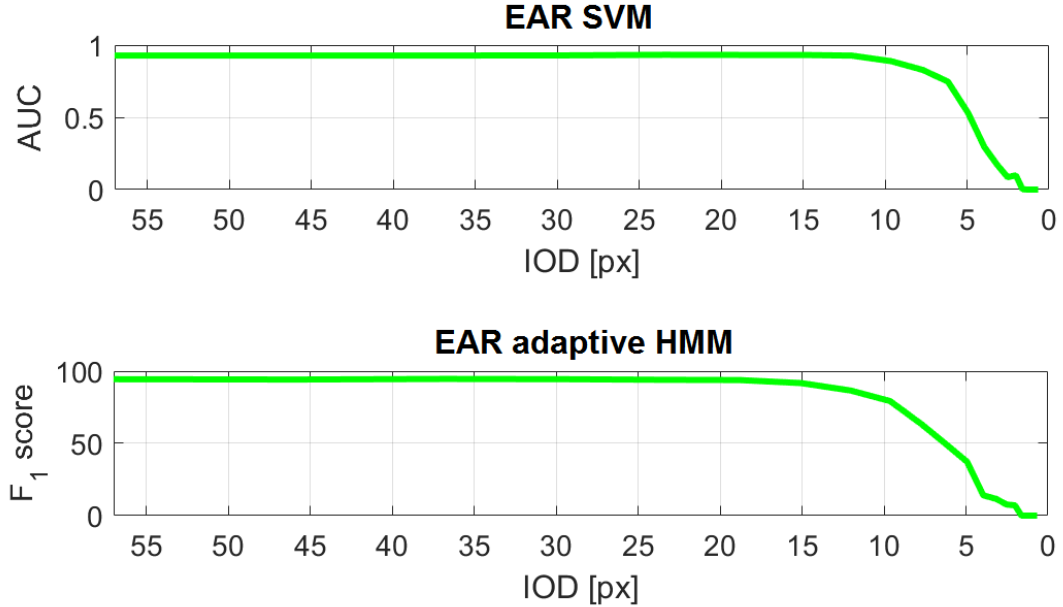


Figure 5.13 The results of the blink detectors as a function of IOD. Top plot shows areas under precision-recall curves for EAR SVM method and bottom plot show F_1 (5.4) scores for EAR adaptive HMM method.

5.2.5 Experiments on sensitivity of proposed blink detectors

Change of resolution

The face resolution can be described by an indicator called inter-ocular distance IOD which is a distance in pixels between centers of eyes. This experiment investigates the robustness of the detectors with a decreasing IOD.

We iteratively decrease image resolution to 80 % of size of previous image and measure the accuracy of the blink detectors. The experiment is done at ZJU dataset. All the subjects from the ZJU dataset are recorded in a similar lighting conditions and the distance of camera is also almost constant. The average IOD is 57.4 px on original images. We subsample images to have average $IOD \in \{57.4, 45.9, 36.7, \dots, 1.3, 1.0\}$ pixels. We get facial landmarks at the resized images using Intraface [6] landmark detector. The face detector is unable to initialize the detection for images with resolution lower than about 10 pixels of IOD. To solve this, we provide a face detector with the first frame of each video at original resolution and further the detector tracks the landmarks on subsampled images. Other frames except the first one do not have access to the original resolution. Alternatively, external face detector can be used to initialize.

The accuracy of blink detectors while decreasing the resolution is computed on both the proposed methods EAR SVM and EAR adaptive HMM. While evaluating EAR SVM, for each resolution, the precision-recall curve is computed by spanning an SVM threshold. For AUC computation, the curve is adjusted such that points being worse in both the precision and the recall than some other points in the precision-recall curve are

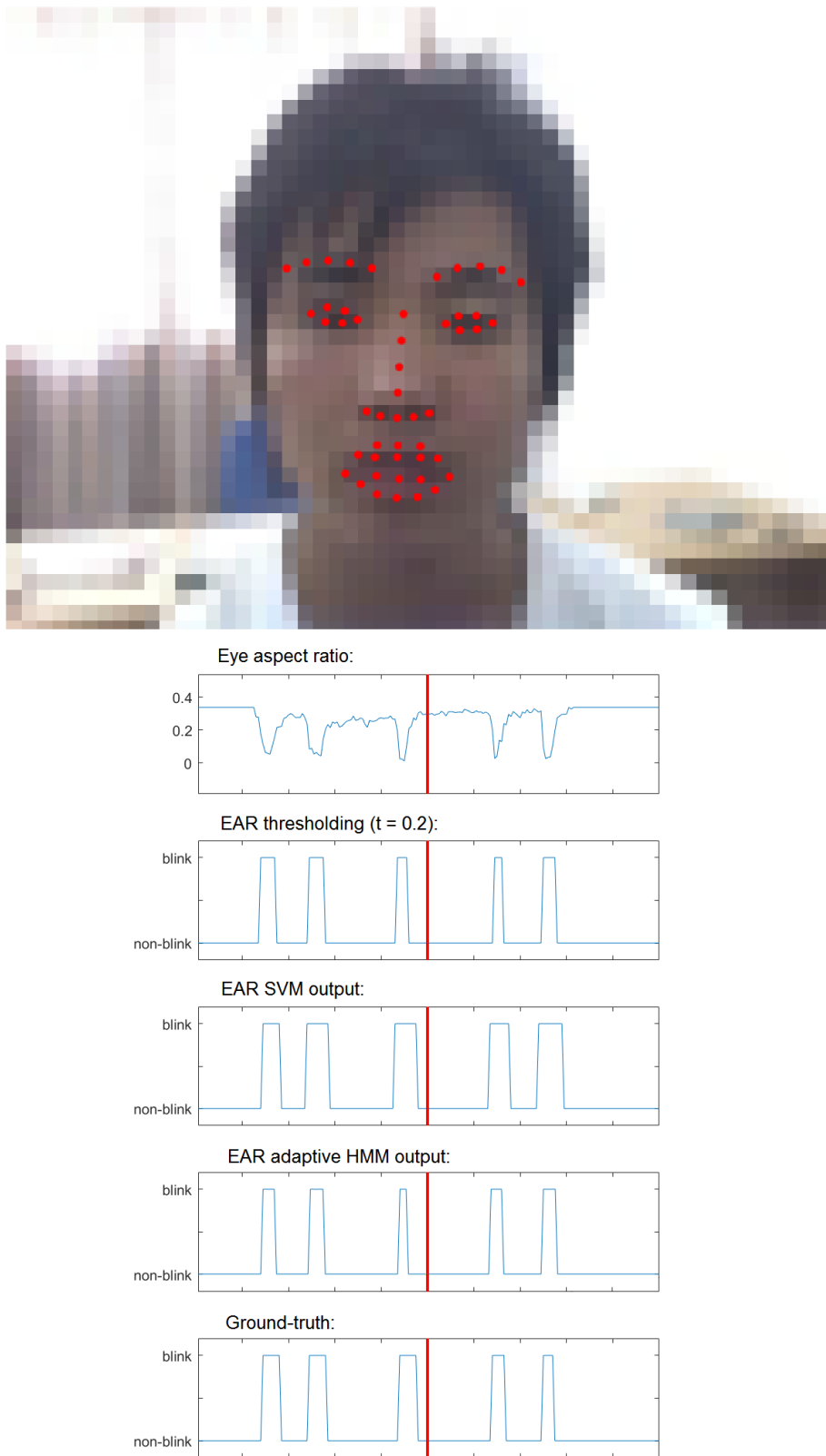


Figure 5.14 Example of detected blinks at small resolution of 9 px of IOD. The plots of the eye aspect ratio EAR in Eq. (4.1), results of the EAR thresholding (threshold set to 0.2), the blinks detected by EAR SVM, the blinks detected by EAR adaptive HMM and the ground-truth labels over the video sequence. Input image with detected landmarks (depicted frame is marked by a red line). All blinks were detected correctly by all the proposed methods.

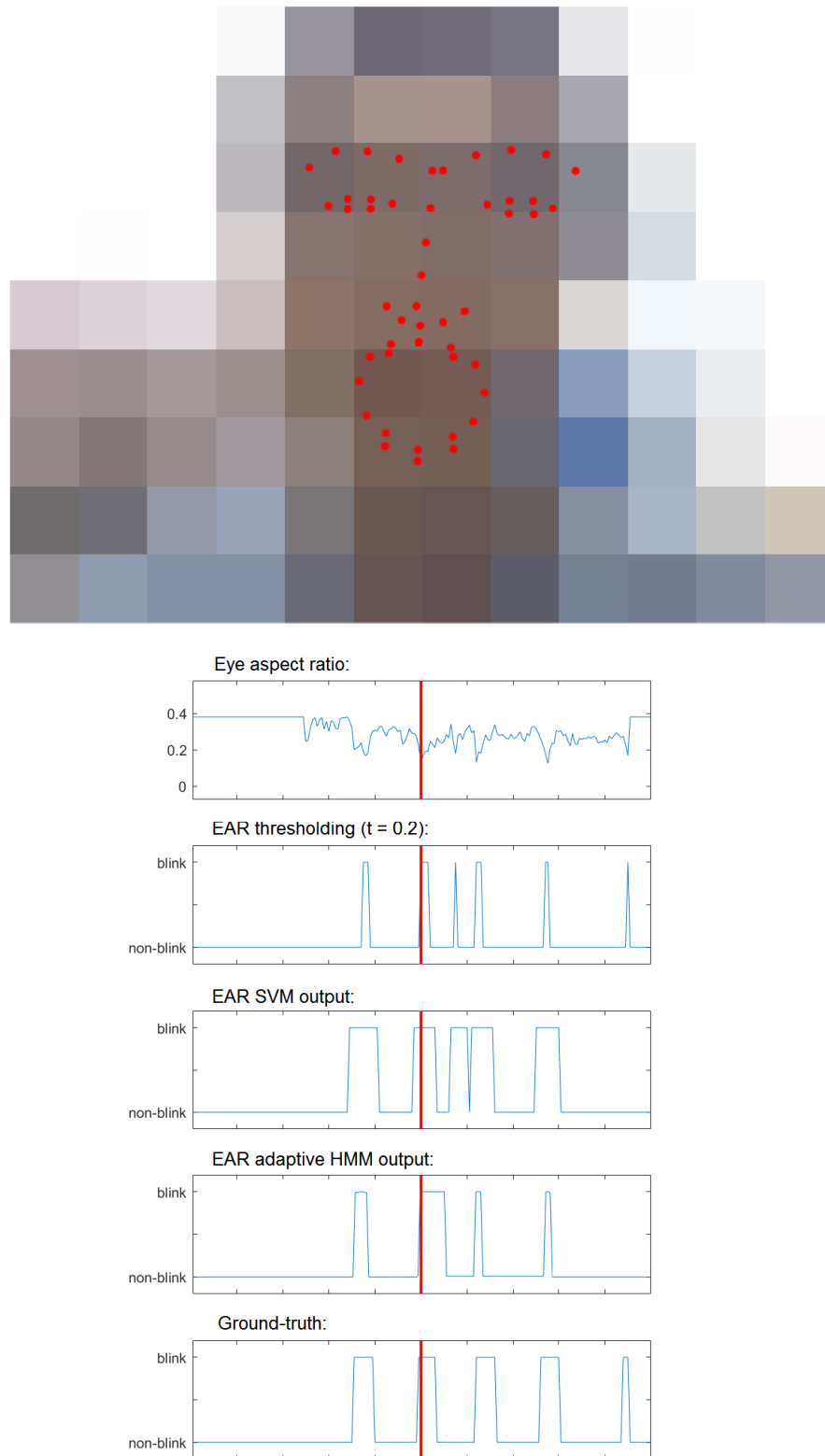


Figure 5.15 Example of detected blinks at extremely small resolution of $IOD = 2.5$ px. The plots of the eye aspect ratio EAR in Eq. (4.1), results of the EAR thresholding (threshold set to 0.2), the blinks detected by EAR SVM, the blinks detected by EAR adaptive HMM and the ground-truth labels over the video sequence. Input image with detected landmarks (depicted frame is marked by a red line). Most of the blinks were detected correctly by the proposed methods.

filtered out. The AUC is depicted in a top plot of Fig. 5.13. There is no precision-recall curve while evaluating EAR adaptive HMM because we obtain only one precision-recall point for each resolution. The F_1 score (5.4) is computed and plotted in a bottom plot of Fig. 5.13.

Until the IOD = 15 px both the detectors are excellent. Then the EAR adaptive HMM method starts to slowly decrease its performance. The EAR SVM holds a very good result up to IOD = 10 px which is really surprising. See example in Fig. 5.14 where all blinks were correctly detected even at IOD = 10 px.

Astonishingly, there are videos at which blink detectors partly work as low as IOD is 2.5 px. Interpret an image/video in such a low resolution is difficult for human. An example is shown in Fig. 5.15. All the proposed methods correctly determined 4 blinks from 5. They have at most two mistake, but the last blink should not be computed, because it is not the full blink. The landmarks are not obviously accurate at all but they still reflect a movement of eyelids and thus they also reflect a change of EAR.

The facial landmark detectors are very precise even at low resolution. Further effort to improve an estimation of a level of eye openness directly from image may be very difficult. Ability of the blink detector to work with low resolution images allows possible applications where a consumer webcam or a surveillance camera are used. Blinking of a subject is monitored in a surprisingly large distance for even a group of people.

Change of frame rate

The dependence of detector accuracy on frame rate is tested at this experiment. The videos are transformed to different frame rates by omitting some frames. This may be a little bit different from decreasing frame rate due to long camera exposure which may produce blurred images. So the new frame rates are set to be divisors of original frame rate. The 30fps videos are transformed to have 30, 15, 10, 6, 5, 3, 2 and 1 frame per second and 100fps videos have new frame rates equal to 100, 50, 25, 20, 10, 5, 4, 2 and 1. The experiment is done on the ZJU, Eyeblick8 and Silesian datasets. The results for higher frame rate than 30 fps at Silesian dataset are not shown because they almost do not change.

Fig. 5.16 show results of EAR SVM blink detector in dependence of frame rate. The EAR SVM method does not produce one precision-recall point so the area under the precision-recall curve is computed for each frame rate. The AUC is computed in the same way as while evaluating change of IOD experiment. The results of EAR adaptive HMM method are shown in Fig. 5.17. The F_1 score (5.4) is evaluated for each frame rate.

We can see that both the curves in Fig. 5.16 and Fig. 5.17 showing the accuracy of the detectors are very similar. The accuracy is almost unchanged until 10 fps. Then it begins slightly worsen and from 5 fps it fails quickly. So the conclusion is that both EAR SVM and EAR adaptive HMM methods work very well until frame rate of 10 fps.

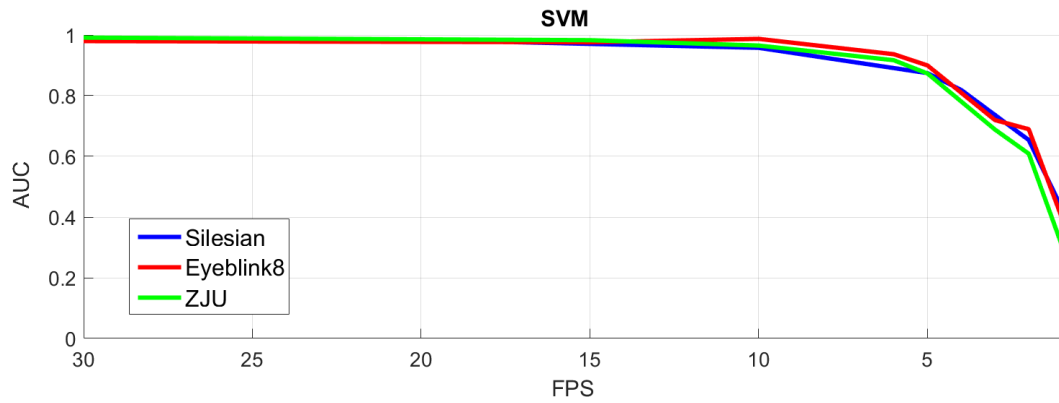


Figure 5.16 The area under precision-recall curve computed for iteratively decreasing frame rate using EAR SVM method.

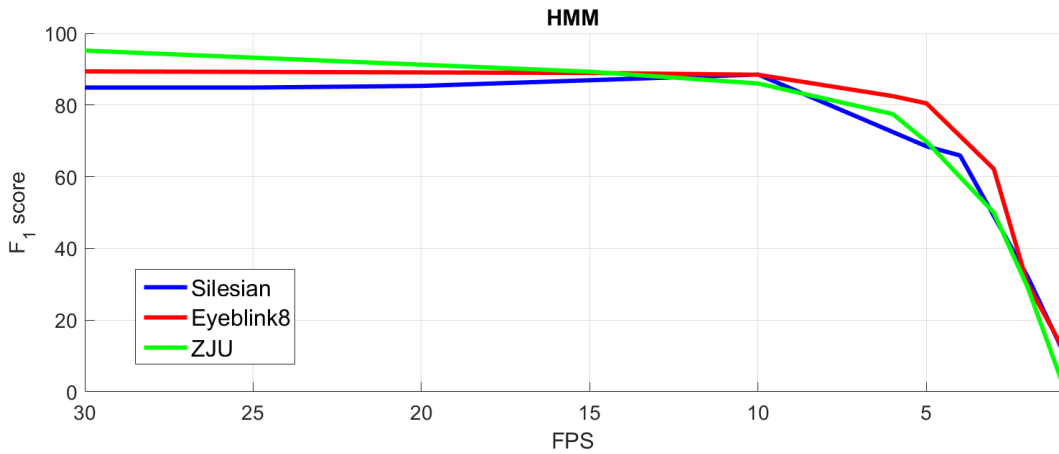


Figure 5.17 The F_1 score computed for iteratively decreasing frame rate using EAR adaptive HMM method.

6 Eye blink detector application

I explore drowsiness during the day as an application of the eye blink detection. I recorded short videos of myself working on a laptop. My drowsiness is estimated from blink characteristics such as frequency and average duration.

I recorded 1-minute long videos during the day. I used a web camera on my laptop and a web camera Logitech C920 that both recorded in 640×480 px resolution. These cameras, especially the built-in web camera, are of a consumer quality. There is a lot of noise and very poor contrast and sharpness, particularly in a weak night illumination. The frame rate depends on an illumination and on a computer workload but it varies from 8 to 30 fps. The recording was triggered randomly in about 15 minutes intervals. I was not aware exactly while I was recorded. I collected the videos for 10 days while I was intensively working on my diploma thesis. The video sequences are quite challenging because of varied head poses, face occlusions and poor quality of images. I often look on a keyboard and sometimes I look on a screen, for a very short time on a keyboard and again on a screen which may have been misinterpreted as blinking. Surprisingly, I found out that I frequently subconsciously put my hands on face, most often on my mouth or my nose. These occlusions may be distracting for the landmark detector. Examples of video frames with various illumination, occlusions and noise are shown in Fig. 6.1 .

All the videos having detected face less than 80% of the time were discarded. It happened mostly when I was out of field of view of the camera and I forgot to stop recording or when I wrote something on a table and I had bent down my head for most of time of the 1-minute recording. The Intraface [6] system is used to detect facial landmarks. Both the eye blink detection method proposed in Sec. 4.1 and Sec. 4.2 are applied. A day is divided into 24 bins where 1 bin represents 1 hour. The videos were recorded from 7 a.m. to 1 a.m. of the following day. There were recorded from 4 to 35 videos for each hour, averagely 15 videos per hour, in total 355 1-minute videos.

A commonly used drowsiness identifier PERCLOS¹ [36] is not suitable for monitoring fatigue of a subject working on a laptop because of frequent looking down on a keyboard. This could be misinterpreted from a view of the camera as closed eyes. So we use an average blink frequency and duration as main drowsiness indicators for all the videos. The results are assigned to the bins according to a time of the recording. The duration is computed using EAR adaptive HMM method, because EAR SVM method cannot correctly determine a blink length. The frequency is computed by both the EAR SVM and EAR adaptive HMM and averaged.

¹PERCLOS determines a time having closed eyes at least 80%



Figure 6.1 Various examples of video frames used for eye blink drowsiness application.

Let us define a relative drowsiness index κ as a function of average blink frequency F (blinks per minute) and duration Z (in ms) computed for each hour during a day. The frequency and the duration are normalized to have zero mean and standard deviation equal to one. The formula for calculation κ is chosen so that the frequency and duration have the same weight:

$$\kappa = F_{norm} + Z_{norm}. \quad (6.1)$$

The drowsiness index κ of the recorded videos is shown in Fig. 6.2. I can fairly confirm the measured drowsiness index curve which corresponds to my subjective feelings. I usually have slow mornings and it starts to get better at about 10 a.m.. After having lunch, the afternoon is almost balanced but I can honestly say that at about 9 p.m. I work best. This corresponds to the measured drowsiness index which starts to get lower at 8 p.m. and from 11 p.m. it grows quickly.

The means and standard deviations of blink frequency and blink duration computed at collected videos are depicted in Fig. 6.3. The standard deviations are quite big which may be caused by the fact that the activities are changed within one hour, e.g. blink frequency while reading differs from blink frequency while thinking or writing.

We note that the blink measurements may not be completely accurate because sometimes the videos are only about 10 fps due to long camera exposure while having poor lighting conditions. Nevertheless, this simple experiment confirms that the drowsiness may be monitored by simple blink characteristics such as blink duration and blink frequency.

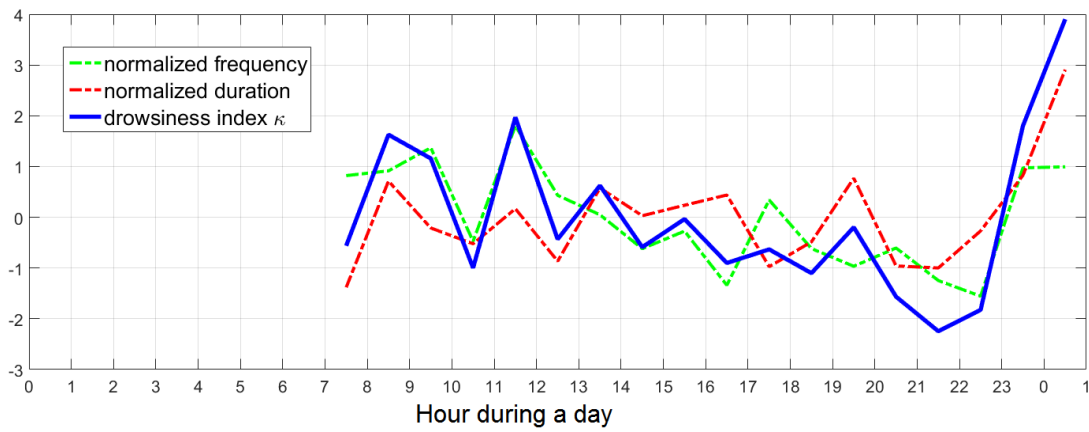


Figure 6.2 Blink characteristics of a subject working on her diploma thesis measured each hour during a day. A result is averaged from 10 days. Normalized blink frequency (green) per minute is computed and averaged from EAR SVM and EAR adaptive HMM outputs. Normalized blink duration (red) is computed using EAR adaptive HMM method. Drowsiness index (blue) as a function of normalized blink frequency and normalized blink duration.

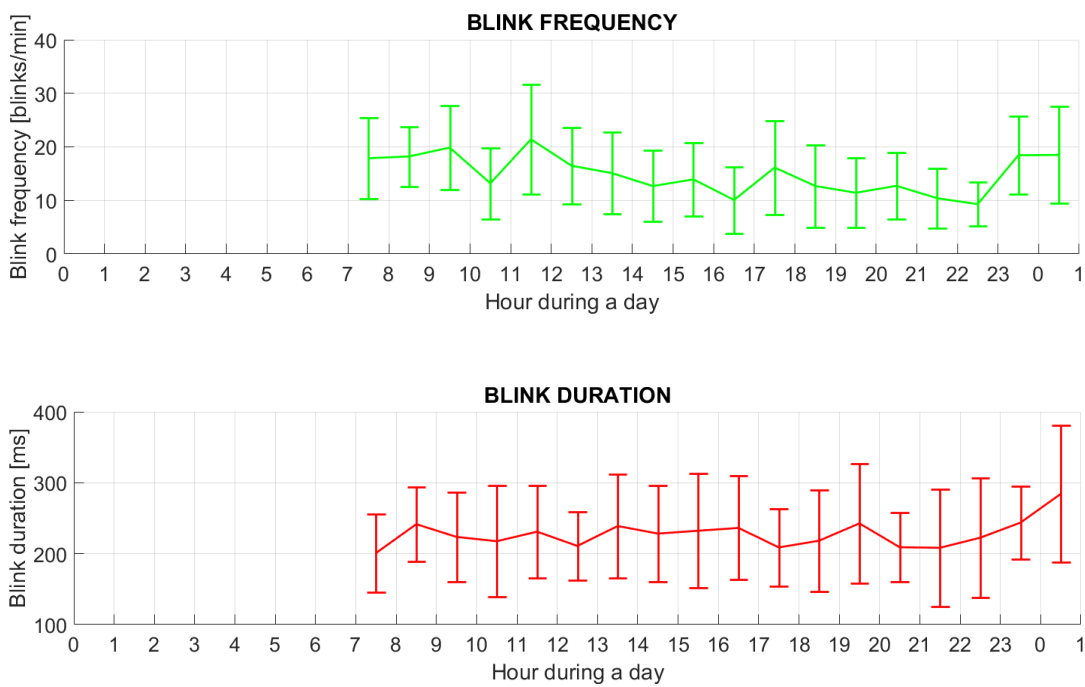


Figure 6.3 Blink frequency and blink duration over the day. The plots have errorbars of standard deviation.

7 Implementation details

A processing time is computed using Eyeblick8 dataset which is recorded in a resolution of 640×480 px and have IOD about 62.9 px. An average time for processing one frame using EAR SVM is 19.2 ms and using EAR adaptive HMM it is 18.7 ms. These times already include a processing time taken for finding facial landmarks. Thus the proposed algorithms run in about 50-60 fps while using ordinary laptop (64-bit Windows 8, Intel Core i7-5500U@2.4 GHz, 8GB RAM).

A real-time blink detector demo has been prepared. It runs in Matlab and uses OpenCV to capture images from a laptop webcam. A beep sounds when a subject being in a field of view of a camera blinks.

The main part of the work is programmed in Matlab R2015b. Some parts, especially collecting of videos of myself for the application, are written in C++. The OpenCV [52] library is used for capturing and processing images. The recording of videos is done using standard built-in laptop webcam and Logitech C920 webcam. The text is written in \LaTeX in online environment Overleaf [53].

8 Conclusion

Real-time eye blink detection algorithms were introduced. We quantitatively demonstrated that regression-based facial landmark detectors are precise enough to reliably estimate a level of eye openness. While they are robust to low image quality (low image resolution in a large extent) and in-the-wild phenomena as bad illumination, facial expressions, etc.

Two methods for blink detection were proposed. Both methods use a single scalar quantity, eye aspect ratio, estimated from landmark locations detected for each frame of a video sequence. The eye blink detection based on an SVM classifier, that takes a temporal window of the EARs, is presented in the first method. The second approach uses a hidden Markov model to decide between the open and closed eye states. A simple state machine detecting blinks according to eye closure lengths is then deployed. Finally, the HMM based method is equipped with an adaptation mechanism that adjusts model parameters to fit well to a subject being observed over time.

The proposed methods were thoroughly experimentally tested and qualitatively evaluated on three standard datasets. A comparison with a baseline EAR thresholding as well as with several state-of-the-art algorithms proved competitive results. The SVM based method outperforms method using HMM except for the ZJU dataset where the methods have almost the same result. On the other hand, the HMM method can be used even when recognizing eye closures longer than average eye blink which cannot be done by SVM approach. Another advantage of the HMM based method is that it is unsupervised unlike the SVM method which needs annotated training data.

The proposed algorithms run in real-time (50 fps), since the additional computational costs for the eye blink detection are negligible besides the real-time landmark detectors.

We see a limitation in the eye openness estimate. While EAR is estimated from a 2D image, it is fairly insensitive to a head orientation, but it may lose discriminability for out of face rotations. A solution might be to define the EAR in 3D. There are landmark detectors that estimate a 3D pose (position and orientation) of a 3D model of landmarks [8, 7].

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