Anytime learning for the NoSLLiP tracker

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1. Introduction

Visual tracking is the process of repeated estimation of the state of an object given an image and the state(s) in previous frame(s). The state of an object is a set of parameters determining its pose (e.g. position, scale, rotation) and/or appearance. The most popular tracking approach is the Lucas–Kanade class of trackers [1,7] which minimizes the sum of intensity differences between a template and image data by the Gauss–Newton gradient descent optimization method. The intensity function is locally approximated by the first-order Taylor expansion and motion parameters are estimated as a linear function of image-template differences. The linear function is expressed as the pseudo-inverse of a matrix which is a function of image gradients. Like any other gradient method, the Lucas–Kanade tracker suffers from convergence to a local minimum, an unknown number of required iterations and an unknown basin of convergence.

Cootes et al. [2] noticed that a similar minimization task is solved in each frame and proposed to replace the pseudo-inverse operation with a multiplicative matrix learned on a set of synthetically perturbed examples, see Fig. 1. Cootes’ method [2] predicts motion parameters as a linear function of object intensities; we call such methods learned linear predictors (LLiP). A LLiP method was adapted by Jurie and Dhome [4] for tracking of rigid objects. Unlike Cootes et al. [2], Jurie’s LLiPs are used for prediction of local 2D translations only. This approach has recently attracted interest of the tracking community [3,12] and it has been also generalized to non-linear prediction as demonstrated by Williams et al. [9], who learn the predictor by a Relevance Vector Machine.

Staying in the realm of trained trackers, we proposed [11] a tracker that consists of a Sequence of LLiPs (SLLiP), see Fig. 2. Since the time required for motion prediction by a SLLiP directly corresponds to the number of used pixels, only a small subset of pixels from a template is used. The SLLiP learning is formulated as an optimization problem where time of tracking (computational complexity) is minimized given a predefined precision of motion predictors. In [11], a globally optimal solution is delivered, the learning might be prohibitively time consuming for large problems.

The main contribution of this paper is a new anytime learning approach which, after a very short initialization period, provides a solution with predefined precision. The solution is continuously improved, i.e. the SLLiPs with lower complexity and defined precision allowing for faster tracking are continuously delivered. The anytime learning searches through the space of SLLiPs and successively constructs SLLiPs from LLiPs of different complexities. In order to make the searching process efficient, the branch and bound [5] searching approach is used.

If no constraint on the learning time is imposed, the anytime learning algorithm finds a globally optimal solution with respect to a certain class of predictors. If time consuming learning is not acceptable, the tracking can start immediately after a short initialization period. Since the SLLiP tracking requires only a fraction of processing power of an ordinary PC, the learning can continue in parallel background thread.

We consider only linear predictors, nevertheless, the method is easily extended to an arbitrary polynomial class by data lifting. For instance, particular monomials can be considered as additional features.
2. Problem formulation

In this section, we introduce formal definitions of LLiP and SLLiP and formulate their learning as a constrained optimization problem. Let us suppose we are given an image $I$ of an object to be tracked. Object motion is robustly determined by RANSAC from local algorithms is presented. Section 4 compares learning/tracking time, robustness and accuracy of the proposed approach with state-of-the-art approaches [4,6,7,11] on ground-truthed sequences. Section 3.2 describes how a training set is constructed from a single image. In Section 3.1 the proposed anytime learning algorithm is introduced, then

The rest of the paper is organized as follows: Section 2 summarizes properties of SLLiPs [11] and introduces notation and definitions. Section 3.1 describes how a training set is constructed from a single image. In Section 3.2 the proposed anytime learning algorithm is presented. Section 4 compares learning/tracking time, robustness and accuracy of the proposed approach with state-of-the-art approaches [4,6,7,11] on ground-truthed sequences. Section 5 concludes the paper.

2. Problem formulation

In this section, we introduce formal definitions of LLiP and SLLiP and formulate their learning as a constrained optimization problem. Let us suppose we are given an image $I$ of an object to be tracked. Object motion is robustly determined by RANSAC from local motions of some points on the object. These points are called reference points and their motion is estimated from their neighborhood. For motion predictors, it is not necessary to use all neighborhood pixels, because sufficient precision is achievable even with smaller number of pixels. Therefore only a selected subset of pixels $X = \{x_1, \ldots, x_n\}$, called support set, is used. LLiP estimates motion of the reference point from the intensities observed on the support set. These intensities are stored in the observation vector denoted $I(X)$.

We denote $(t \circ X)$ the support set warped by a motion with parameters $t$. For example, if the considered motion is a 2D translation, then $(t \circ X) = (X + t) = \{x_1 + t, \ldots, x_n + t\}$. There is a mapping (rendering) from parameters $t$ to observations $I(t \circ X)$, which is usually not invertible. We therefore search for a mapping approximating a the set of motions $t$ which could have generated the observation $I(t \circ X)$. This mapping assigns a $p$-vector of motion parameters to a $c$-vector of observation.

**Definition 1.** Linear predictor (LLiP) is an ordered pair $\phi = (\mathcal{H}, X)$, which assigns $p$-vector of motion parameters $t = \mathcal{H}(X)$ to $c$-vector of observations $I(X)$, where $\mathcal{H} \in \mathbb{R}^{p \times c}$.

All predictors $\phi$ are characterized by the following parameters, see also Fig. 3:

**Definition 2.** Complexity $c(\phi)$ of predictor $\phi$ is the cardinality of the predictor’s support set $X$.

**Definition 3.** Range $R(\phi)$ of the predictor $\phi$ is a set of motion parameters.

**Definition 4.** Error of predictor $\phi = (\mathcal{H}, X)$ for range $R(\phi)$ is $E(\phi) = E(||t - \mathcal{H}(t \circ X)||^2)$. $t \in R(\phi)$, where $E(\cdot)$ denotes the expectation value with respect to $t$ uniformly distributed on $R(\phi)$.

Predictor complexity approximately corresponds to the number of multiplications and sums necessary for motion estimation. It is clear that there is no ideal predictor which would simultaneously has (very) low complexity, (very) large range and (very) small error. It is easy to see that the higher the complexity the better the prediction. However, as the complexity increases towards the complete template, the improvements become less and less significant. In general, for large ranges it is very difficult to achieve a good prediction with any complexity. In order to overcome this limitation we develop a sequential predictor $\Phi = (\phi_1, \ldots, \phi_m)$. Since the sequential predictor is provably superior to a single monolithic predictor, it allows lower complexity for higher precision. A vector of motion parameters $t$ is predicted in $m$ steps as follows:

\[
\begin{align*}
t_1 & = H_1(I(X_1)), \\
t_2 & = H_2(I(t_1 \circ X_2)), \\
t_3 & = H_3(I(t_2 \circ X_3)), \\
& \ldots \\
t_m & = H_m(I(t_{m-1} \circ X_m)), \\
t & = \bigcap_{i=1}^{m} t_i.
\end{align*}
\]

The first vector of motion parameters $t_1$ is directly predicted from intensities observed at locations defined by the support set $X_1$. The second predictor estimates motion parameters $t_2$ from intensities $I(t_1 \circ X_2)$ observed on the its support set warped by $t_1$, and so on. The advantage is that each predictor in a sequence is more and more specific, using a smaller range which corresponds to the accuracy of the preceding predictor.

**Definition 5.** Sequential predictor (SLLiP) is an $m$-tuple $\Phi = (\phi_1, \ldots, \phi_m)$ of predictors $\phi_i \in \omega$, $i = 1 \ldots m$, where $\omega$ is a set of predictors.

\[\text{In practice, the error is the mean value of square Euclidean error of all predictions from the range.}\]
The set of predictors \( \omega \) can include all possible predictors, or its convenient subset. Because of computational complexity of the learning process, only the predictors with \( H \) minimizing their prediction error for a given support set and training set, will be further considered.

**Definition 6.** Optimal sequential predictor is a sequential predictor

\[
\phi^* = \arg \min_{\phi \in \omega^m} \left\{ \sum_{i=1}^{m} c(\phi_i) | \lambda(\phi_m) \leq \lambda^* \right\},
\]

where \( \lambda^* \) is predefined prediction error, \( c \) is predictor complexity, \( \omega \) is a set of predictors and \( \omega^m = \omega \times \omega \times \cdots \times \omega \) is a set of sequential predictors of length \( m \).

3. Anytime learning of SLLiP

We define learning as a search for the optimal SLLiP subject to a predefined prediction error (Definition 6). In general, the learning procedure consists of two steps: support set selection and SLLiP optimization. The support set selection is a combinatorial problem, the solution of which might be time consuming [8,10]. Since we are interested in applications where the learning time is an issue, a randomly selected support set is used instead. The SLLiP optimization is also simplified by restricting \( \omega \) to be a class of LiPs with the minimal prediction error (Definition 4). Nevertheless, the proposed learning algorithm can be used to find the globally optimal solution with respect to arbitrary \( \omega \). For example, \( \omega \) could be a set of LiPs learned by the minimax method, then the result of learning would be the same as of the algorithm proposed in [11].

Note that the globally optimal solution found with respect to the restricted \( \omega \) is not guaranteed to provide globally optimal solution with respect to the set of all possible LiPs. In Section 3.1, training set construction from a single image is described. Section 3.2 then presents SLLiP learning.

3.1. Training set construction

Given a predefined range of motions within which the tracker is assumed to operate, we perturb the support set by motion with parameters \( q_i \) randomly (uniformly) generated inside the range. Each motion \( q_i \) warps the support set \( X \) to a set \( X_i \), where a vector of intensities \( I_i \) is observed, see Fig. 4. Given the observed intensities, we search for a mapping assigning motion \( t_i = (q_i)^{-1} \), which warps \( X_i \) as close as possible to the original support set \( X \). These examples are stored in matrices \( I = [I_1 \cdots I_d] \) and \( T = [t_1 \cdots t_d] \). The ordered triple \( (I, T, X) \) of such matrices and ordered \( d \)-tuple of support sets \( X = \{X_1 \cdots X_d\} \) composes a training set.

3.2. Learning algorithm

In this section, we describe the method searching for the optimal sequential predictor given a training set \( (I, T, X) \) generated on image \( I \). Since we restricted the set of considered LiPs \( \omega \) to the set of LiPs minimizing prediction error \( \lambda \), the LiP learned from the training set is \( \phi = (H^*, X) \), where

\[
H^* = \arg \min_{H \in \mathbb{R}^{d \times d}} \| H I - T \|^2_2 = T^+ I^T \tag{3}
\]

and \( X \) is the support set aligned with the object.

Fig. 4. An image patch is perturbed by the motion parameters within a predefined range in order to create a set of synthesized examples of observed intensities \( I \) and motions \( t \).
Ideally, the predictor learned according to Eq. (3) would transform intensities $I$ to motions $\tau$. However, this predictor usually does not exist. Therefore the observed intensities are transformed into motion parameters $\tau^{(1)}$ which are as close as possible to the desired motions $\tau$. We warp each support set $X_i \in X$ by motion parameters $\tau^{(1)}$ obtaining the new support set $X_i^{(1)} = \tau^{(1)} \circ X_i$. Denoting $\tau^{(1)}$ the intensities observed on these newly obtained support sets $X_i^{(1)}$, we form the new training set $(\tau^{(1)}, X')$. We refer to it as to training set invoked by predictor $\phi_1$ and denote it $T(\phi_1, c)$, where $c$ denotes the size of support set used in the training set. Similarly, we define training set invoked by sequential predictor as $T(\Phi, c)$.

As already mentioned, the size of the support set influences the prediction error. Removing some pixels from the support set necessarily results in error increase. Given a training set $T(\Phi, c_1)$ we can simply generate a training set $T(\Phi, c_2) = c_2 < c_1$ for the predictor with a lower complexity $c_2$ by removing corresponding number of pixels from $X$ and corresponding number of rows from matrix $I$.

We refer to this process as training set restriction.

In order to simplify the problem, we further work with a discretized set of complexities $C$. The optimal sequence of predictors is found by searching through the set of all SLLiPs, which involve $\sum_{c \in C} |C|$ elements, where $|C|$ denotes the size of $C$ and $m$ is maximum length of SLLiP. In order to make the searching process efficient, the branch and bound [5] searching approach is used. Sequential predictors are successively constructed from the LiPs of different complexities. In the first level, we learn LiPs for all complexities in $C$ according to Eq. (3). They correspond to the SLLiPs of the length equal to one. One of these SLLiPs, $\phi$, is expanded in the next iteration. The expansion means that $\phi$ is successively extended by LiPiPs with different complexities learned on training set invoked by itself $T(\phi, c)$. This process creates $|C|$ new SLLiPs, which could be expanded in further iterations. Once a SLLiP with a sufficiently small prediction error (feasible solution) is found, all other partially constructed SLLiPs with a higher complexity are terminated. i.e. they will never be expanded. The smallest complexity $c'$ of the feasible solution is saved and once any SLLiP reaches a higher complexity it is automatically terminated.

The learning process is summarized in Algorithm 1; see also Fig. 5, which demonstrates six iterations of the algorithm on a toy example with $C = \{20, 300\}$, range equal to 40% of the object size and the predefined error set to 10% of the object size. In the first iteration, two LLiPs with complexities 20 and 300 are learned, denoted $\phi_1$ and $\phi_2$. Obviously, the LLIp with the higher complexity achieves lower prediction error $\lambda(\phi_2) = 0.15$. Since no solution has been found, $\phi_2$ is expanded in the second iteration, i.e. we learn two further LiLPs, denoted $\phi_{21}$ and $\phi_{22}$, on the training set invoked by $\phi_2$. Since both newly constructed SLLiPs $\Phi_1 = (\phi_1, \phi_{21})$ and $\Phi_2 = (\phi_2, \phi_{22})$ achieve sufficiently low prediction error, i.e. smaller than $\lambda = 0.1$, the one with the lower complexity, i.e. $\lambda(\phi_2) = 0.1$, is selected and the other one, $\phi_2$, is terminated. $\phi_1$ could be immediately used for tracking, while the learning can continue: in the third iteration, $\phi_2$ is expanded. Since $\lambda(\phi_2) = 0.1$ and $\phi_2$ is terminated. In the remaining iterations the not terminated SLLiP is further expanded till the solution, SLLiP $\Phi_3$ consisting of 5 LiLPs, is reached. Since the complexity $\lambda(\phi_{21}) = 0.1$ and $\phi_{21}$ is replaced by $\phi_3$. And since there are no more SLLiPs to expand, $\phi_3$ is accepted as the final solution.

Of course, it is likely that better solution exist, consisting from the LLiPs with complexities not constrained to $C = \{20, 300\}$, but this is just a toy example demonstrating the learning process. In practice, we work with $|C| = \{10 \ldots 15\}$.

Algorithm (anytime learning of SLLiP)

Input:
- Range $R$ within which SLLiP is expected to operate.
- Set of considered complexities $C$
- Predefined accuracy $\lambda$.
- Training image $I$.
- Support set $X$.

(1) Set $c = \infty$ (complexity of the simplest admissible SLLiP found) and $i = 0$ (number of current iteration).

(2) Generate training sets $T(c); \forall c \in C$ on the predefined range $R$.

(3) Initialize set $\Omega$ of learned active SLLiPs as a set of LLiPs learned on $T(c), \forall c \in C$ according Eq. (3).

(4) $\Phi = \emptyset, \Omega = \emptyset, \Phi$ (Select and remove $\Phi$ according to a strategy $S$).

(5) For each $c \in C$: (expand $\Phi$)

(a) Generate training set $T(\phi, c)$ invoked by $\phi$.

(b) Learn LLiP $\phi$ for $T(\phi, c)$ according to Eq. (3).

(c) $\Phi' = \phi, \Omega = \Omega \cup \Phi'$ (add the new SLLiP to $\Omega$).

(d) If $c(\Phi') < c'$ then $\Phi' = \Phi'$ and $c = c(\Phi')$ (replace solution).

(e) For each $\phi \in \Omega$ with $c(\phi) > c'$, do $\Omega = \Omega \setminus \phi$ (terminate the SLLiPs with higher complexity).

(6) If $\Omega = \emptyset$ stop otherwise $i = i + 1$ and goto 4.

Output:
- Optimal SLLiP $\Phi^*$

Note that the selection strategy $S$ which selects a SLLiP from $\Omega$ (step 4), may influence the learning behavior. However, if Algorithm 1 satisfies condition $\Omega = \emptyset$ in step 6, $\Phi^*$ is an optimal SLLiP with respect to the set of considered LLiPs $\Omega$. In our implementation, we first use the strategy which expands the SLLiP with the highest complexity. This strategy usually finds a solution $\Phi^*$ in a few iterations. This solution is of a high complexity, but the prediction error is guaranteed and the tracking can start. Then the strategy is switched and the SLLiPs with the average complexity are preferably expanded. Once a solution is reached, it can be immediately used for tracking with a lower performance. If the learning continues, the SLLiP can be in future replaced by better solutions.

The stopping condition (step 6) could be also optionally replaced for example by a maximum number of iterations, maximum running time, maximum depth of the constructed graph or an arbitrary intersection of these conditions. However, such replacement might influence the optimality of the found $\Phi^*$.

4. Experiments

The proposed method is verified on real sequences with planar objects. The object is represented as a Number of SLLiPs (NoSLLiP), which estimates local translations at a few points on the object. Object motion, i.e. a homography, is determined from these local translations by the RANSAC. Note that although we work with planar objects in order to avoid problems of 3D reconstruction, the proposed trackers could be attached to a 3D model with a reasonable texture, as was shown in [11].

The quantitative evaluation of robustness and accuracy of SLLiPs is conducted on sequences with three different objects (MOUSEPAD-MP, TOWEL and PHONE), where ground truth positions of the object corners in total number 11963 frames were manually labeled. Accuracy is measured in each corner as a percentage; the displacement error is related to the current size of the object upper edge. Robustness is

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2 Proof of this claim is detailed in [11].

3 Since the support set is selected randomly its restriction is random as well. If, for instance, the greedy construction [8,10,11] had been used, then the order of the selection would have provided the importance measure of the support pixels and the lastly selected pixels would have been removed firstly in the restriction.

4 We generate only $T^{(c_{max})}$ where $c_{max} - \max C$ is maximum complexity of $C$, the other training sets with the lower complexity are constructed by its restriction.

5 These sequences in conjunction with the ground truth are available at ftp:// cmp.felk.cvut.cz/pub/cmp/data/lintrack/index.html.
measured by the number of loss-of-locks, defined as the cases where the accuracy was worse than 25%. In loss-of-lock frames, the tracker was reinitialized from the ground truth and the accuracy did not contribute to the total accuracy statistic. Some of the successfully tracked frames, which include oblique views, motion blur and significant scale changes, are presented in Fig. 6. The results are summarized in Table 1.

In the first row, results of NoSLLiP tracker with SLLiPs learned by Algorithm 1 with no time constraint (method LS) are presented. Second row contains results for SLLiPs learned by minimax [11] (method MM). The minimax learning minimize the size of a compact region within which all predictions lie (uncertainty region) instead of the square of Euclidean error, therefore higher robustness is achieved, but the learning is 10–20 times longer. Tracking accuracy of MM and LS methods varies with data; the accuracy is similar for MP and TOWEL sequences, but PHONE object contains similar repetitive structure (buttons) which make the LS accuracy significantly worse.

Robustness of the predictor is given by the shape of the error distribution, because the higher the probability of large errors the higher the probability of the predictor failure in the next frame due to its initialization out of its range. Shape of MM SLLiP distribution (blue solid line) and LS SLLiP distribution (red solid line) are shown in Fig. 7. We observe that LS SLLiPs are more likely to have higher errors in difficult cases however, the accuracy in easier cases is higher. In addition to this we can also compare predefined uncertainty region $\lambda_0$ of MM SLLiP, predefined prediction error $c_0$ of

Fig. 5. Demonstration of progress of Algorithm 1 for a toy example with $C = \{20, 300\}$.
LS SLLiP and true error distribution on ground truthed data (MOUSE-PAD sequence). In this experiment we learned 35 SLLiPs with different ranges covering the mousepad. MM SLLiPs are learned to achieve uncertainty region $\lambda_0 = 0.05$ (blue dot-dashed line), LS SLLiPs are learned for prediction error $\varepsilon_0 = 0.03$ (red dot-dashed line). Both the uncertainty region and the prediction error are relative to SLLiPs range. $\lambda_0$, $\varepsilon_0$ were chosen experimentally in order to achieve the best performance of SLLiPs. Lower values result in higher complexity and consequent over-fitting. The error is evaluated on those frames, where inter-frame motion is smaller than the learning range of SLLiPs.

Table 1 compares the NoSLLiP tracker to the state-of-the-art Lowe’s SIFT detector [6] (method: SIFT), Lucas–Kanade tracker [7] (method: LK tracker) and Jurie’s LS LLiP tracker [4] (method: LLiP LS). All these local motion estimators were combined with the RANSAC, to keep test conditions as similar as possible. SIFT tracking mainly fails in frames with strong motion blur or in frames where the object was very far from the camera. LK tracker, which

<table>
<thead>
<tr>
<th>Object</th>
<th>SLLiP learning</th>
<th>Learning time (s)</th>
<th>Processing (fps)</th>
<th>Loss-of-locks</th>
<th>Mean-error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MP LS</td>
<td>11</td>
<td>27.6</td>
<td>17/6935</td>
<td>1.4, 1.3, 1.1, 1.1</td>
<td></td>
</tr>
<tr>
<td>MP MM</td>
<td>310</td>
<td>18.9</td>
<td>13/6935</td>
<td>1.3, 1.8, 1.5, 1.6</td>
<td></td>
</tr>
<tr>
<td>TOWEL LS</td>
<td>16</td>
<td>33.3</td>
<td>2/3229</td>
<td>1.6, 1.8, 1.1, 1.5</td>
<td></td>
</tr>
<tr>
<td>TOWEL MM</td>
<td>310</td>
<td>21.8</td>
<td>5/3229</td>
<td>3.0, 2.2, 1.4, 1.9</td>
<td></td>
</tr>
<tr>
<td>PHONE LS</td>
<td>21</td>
<td>25.6</td>
<td>55/1799</td>
<td>7.3, 7.1, 10.6, 6.5</td>
<td></td>
</tr>
<tr>
<td>PHONE MM</td>
<td>310</td>
<td>16.8</td>
<td>20/1799</td>
<td>1.2, 1.8, 2.6, 1.9</td>
<td></td>
</tr>
</tbody>
</table>

1 Learning time is an average time required per one SLLiP.

Table 2 compares the NoSLLiP tracker to the state-of-the-art Lowe’s SIFT detector [6] (method: SIFT), Lucas–Kanade tracker [7] (method: LK tracker) and Jurie’s LS LLiP tracker [4] (method: LLiP LS). All these local motion estimators were combined with the RANSAC, to keep test conditions as similar as possible. SIFT tracking mainly fails in frames with strong motion blur or in frames where the object was very far from the camera. LK tracker, which

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<th>Processing (fps)</th>
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<tbody>
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<td>1.4, 1.3, 1.1, 1.1</td>
</tr>
<tr>
<td>SLLiP MM [11]</td>
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<td>13/6935</td>
<td>1.3, 1.8, 1.5, 1.6</td>
</tr>
<tr>
<td>SIFT [6]</td>
<td>0.5</td>
<td>281/6935</td>
<td>1.6, 1.2, 1.5, 1.4</td>
</tr>
<tr>
<td>LK tracker [7]</td>
<td>2.6</td>
<td>398/6935</td>
<td>2.3, 2.2, 2.5, 2.5</td>
</tr>
<tr>
<td>LLiP LS [4]</td>
<td>24.4</td>
<td>1083/6935</td>
<td>5.9, 6.0, 6.7, 6.7</td>
</tr>
<tr>
<td>LLiP LS [4] half-range</td>
<td>24.2</td>
<td>93/6935</td>
<td>3.1, 2.3, 2.7, 4.0</td>
</tr>
</tbody>
</table>

Fig. 6. The left column shows images used for training. The middle and right columns demonstrate some successfully tracked frames with strong motion blur from the testing sequences. Blue rectangle delineates the object. Percentage values in corners are current corner speeds related to the current size of the object upper edge.

Fig. 7. Accuracy analysis: Comparison of predefined uncertainty region $\lambda_0$ of MM SLLiPs (blue dot-dashed line), predefined prediction error $\varepsilon_0$ of LS SLLiPs (red dot-dashed line) and true error distribution (blue and red solid lines) on MOUSE-PAD sequence.

We use implementation of the SIFT detector downloaded from http://www.cs.ubc.ca/lowe/keypoints/.
estimates the local motion at Harris corners, provided quite good results on the frames where the object was far from the camera, but its basin of attraction was in many frames insufficient for correct motion estimation, failing for fast motions.

Since we work with a non-optimized implementation of the LK tracker, the presented frame-rate in this experiment could not serve for a speed comparison. Nonetheless the SLLiP computational complexity is clearly smaller than the complexity of the LK tracker. Jurie’s tracker is a LLiP tracker with the support set equal to the whole template learned by LS method for the same reference points and ranges as optimal SLLiPs. Since a single LLiP tracker does not allow sufficient accuracy on the same range, very high loss-of-lock ratio and low accuracy are reported. If the half-range is used, the higher accuracy is achieved, but the number of loss-of-locks is still significantly higher than with NoSLLiP tracker, mainly due to long inter-frame motions.

4.1. Time-constrained learning procedure

The learning procedure proposed in Algorithm 1 might be time consuming if the set of considered LLiPs is too large. Since a long learning time might not be acceptable for some types of applications, either the set of considered LLiPs or the maximum number of iterations have to be restricted. However, the constraint on maximum number of iterations affects the optimality of the found SLLiP, and therefore we show average complexity of the best found solution as a function of iterations in Algorithm 1. Fig. 8 presents this function for different sets of considered LLiPs. One can see that the learning time could be 2–3 times decreased without significant increase of the solution complexity.

Note that there is also another option besides premature interruption of the learning procedure. The anytime learning algorithm, after a short initialization procedure, provides a solution – SLLiP with higher complexity but predefined precision. Having this SLLiP the tracking can immediately start. Since the tracking requires only a fraction of the processing power of an ordinary PC, the learning need not to be necessarily terminated and it might be allowed to run in a parallel background thread continuously providing better and better SLLiPs. This principle theoretically allows to start the tracking procedure immediately without any learning using for example Lucas–Kanade tracker and collect training examples automatically. Once a training set is constructed the learning procedure can run in a parallel thread providing the SLLiPs which continuously replace worse LK trackers. Similar idea based in simple LLiPs was demonstrated in [3].

5. Conclusions

We proposed a fast learning algorithm for the SLLiP learnable tracker [11]. Unlike the original learning procedure, the new algorithm has the anytime property and outputs progressively faster SLLiPs satisfying a user defined accuracy and range. The learning process very quickly returns a SLLiP which is slow, but satisfies the user-defined conditions on accuracy and range. During tracking, the learning is run in a background thread and gradually improves the SLLiP tracker.

The method was qualitatively evaluated on approximately 12,000 labeled frames with three different planar objects. The performance and robustness superiority of the SLLiP tracker in comparison with Lucas–Kanade tracker [7], SIFT detector [6] and Jurie’s LLiP tracker [4] was demonstrated. We encourage the reader to download sequences, ground-truth data and a MATLAB implementation which is available at http://cmp.felk.cvut.cz/demos/Tracking/lintTrack.

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